

# Modeling microbial dynamics in food processes

An experiment design approach to  
predictive microbiology

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# Outline

- 1. Predictive microbiology**
  - 2. (Predictive) model building cycle**
  - 3. Kinetic models**
    - *Optimal Experiment Design (OED)*
      - Case study 1: effect of T on  $\mu_{\max}$
    - *Design Of Experiments (DOE)*
      - Case study 2: effect of several factors on  $\mu_{\max}$
- 
- 1. Probabilistic models**
    - *Data collection*
    - *Model building*

# Predictive microbiology

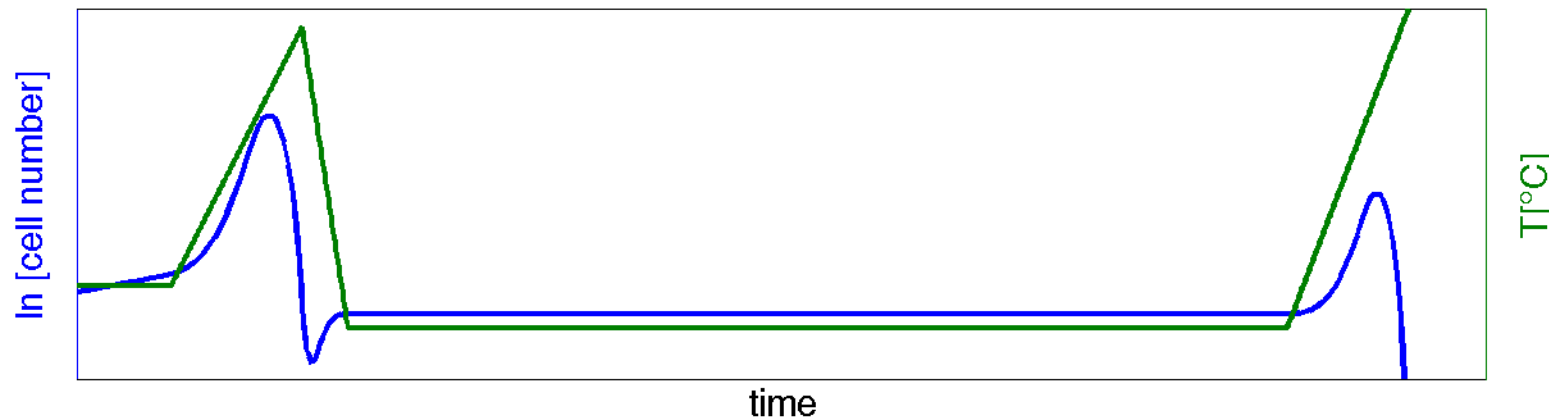
Microbial food safety  
and quality



Reduction and/or prevention of  
microbial growth

Microbial dynamics are determined  
by the environmental factors.

⇒ temperature



# Predictive microbiology

## Predictive microbiology

⇒ mathematical modelling of **microbial dynamics** (growth, survival, inactivation, growth/no growth) under **changing environmental conditions** (e.g., temperature, pH,  $a_w$ )

⇒ predict microbial dynamics in **foods**

⇒ control food safety & food quality

## Specific use

- **food process industry** (e.g. formulation of new products)
- **regulatory bodies** (e.g. storage guidelines, food handling)
- **risk assessment** in the food trade

# Predictive microbiology

## *The model building cycle*

A priori knowledge

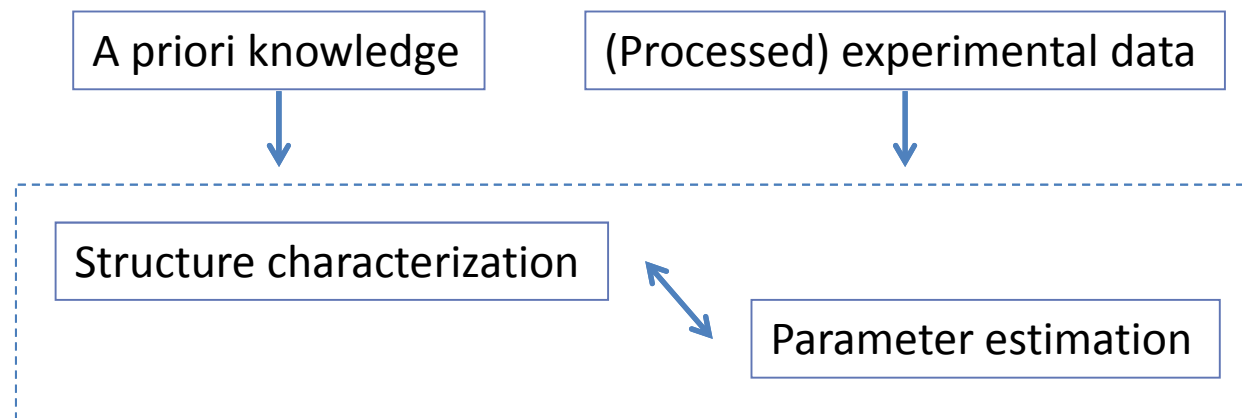


(Processed) experimental data



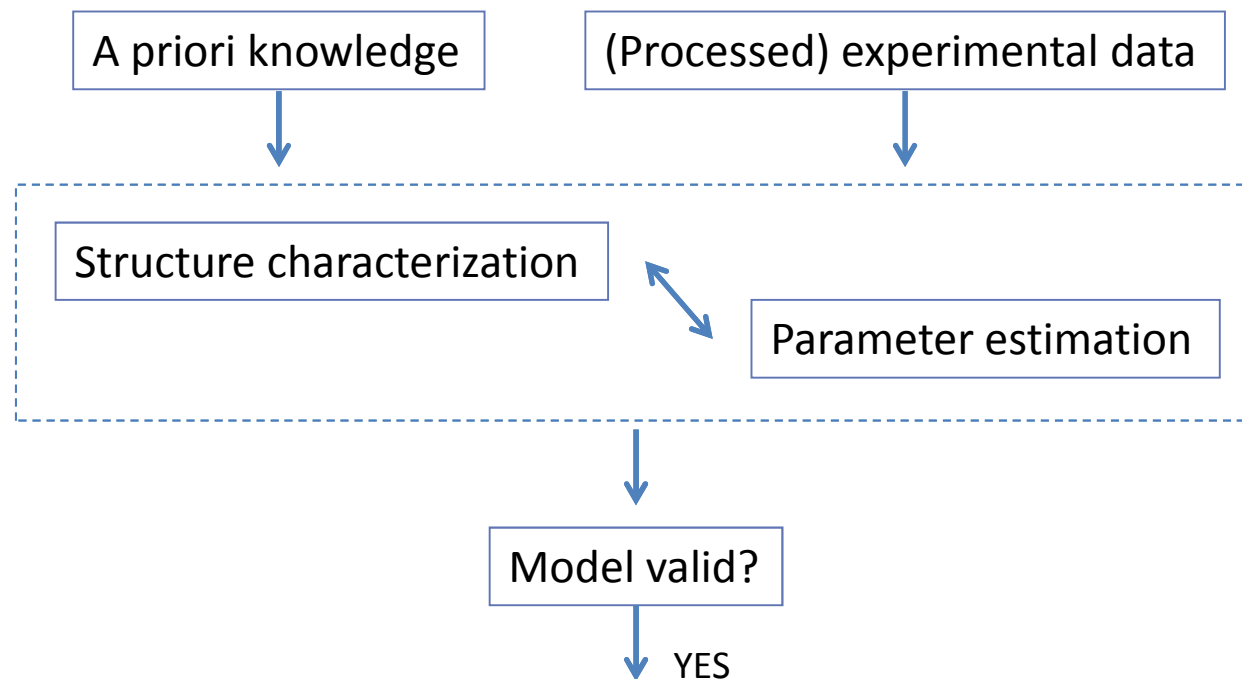
# Predictive microbiology

## *The model building cycle*



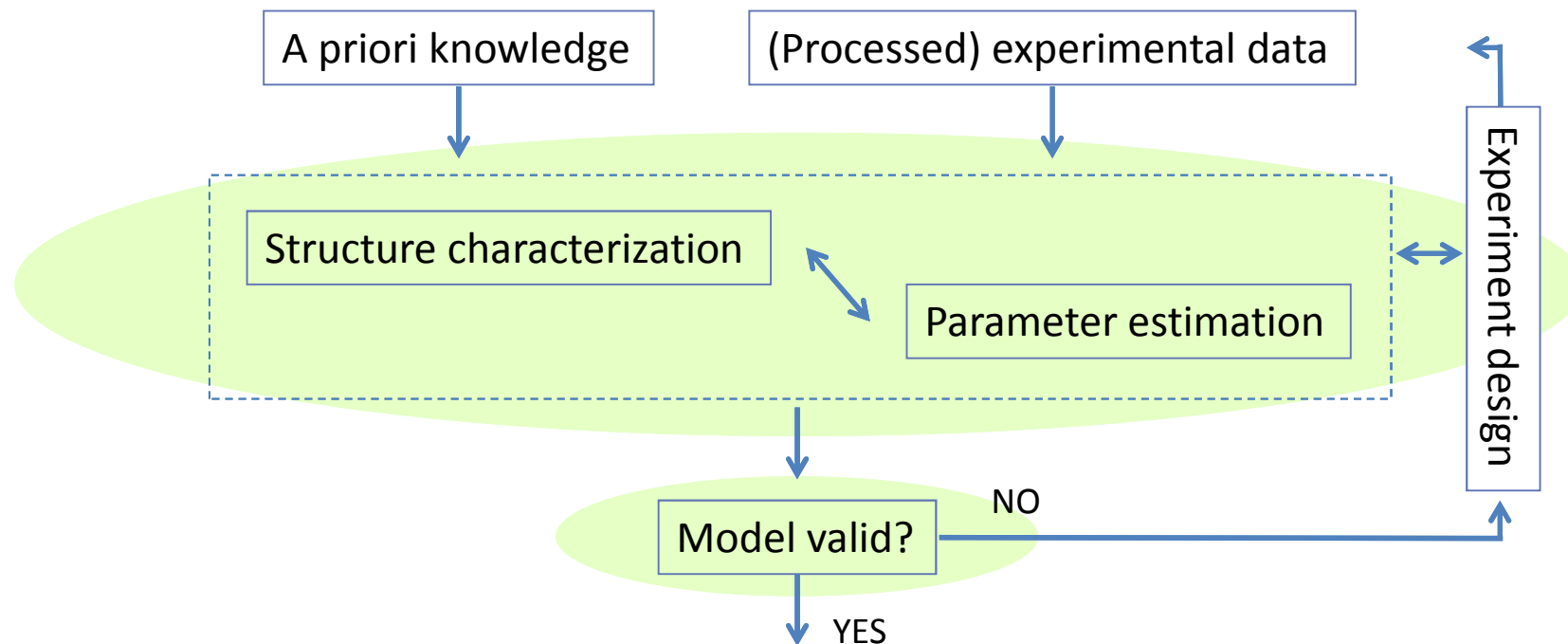
# Predictive microbiology

## *The model building cycle*



# Predictive microbiology

## *The model building cycle*

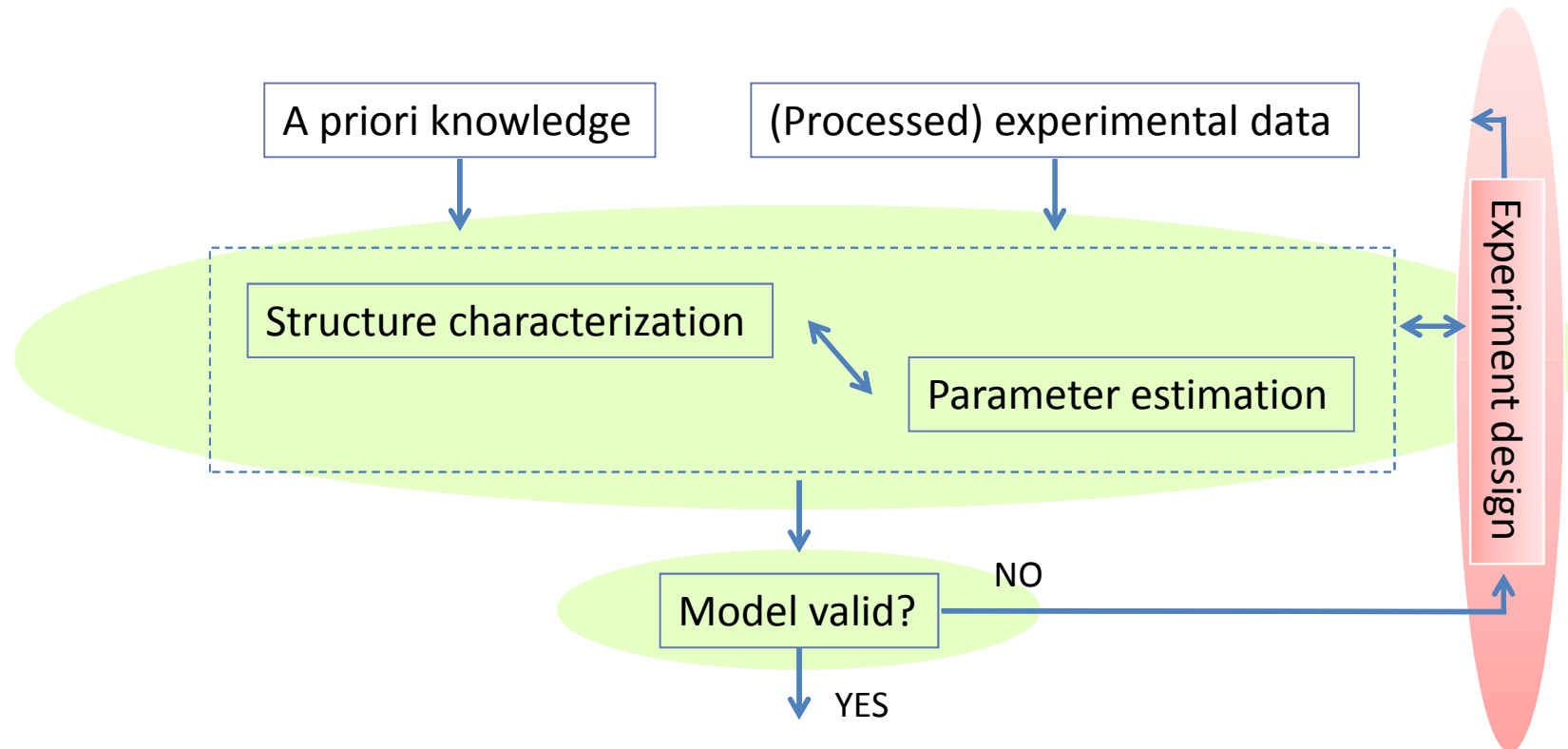


**=> Model building is a data-driven process**



# Predictive microbiology

## *The model building cycle*



**=> Model building is a data-driven process**

**=> Well-founded design improves model quality and validity**

# Predictive microbiology

## *Importance of data acquisition*

This presentation will outline the importance of *adequate* data collection when building/improving predictive models for food processes.

## 1. Kinetic models

- Techniques to improve parameter estimation accuracy
  - Optimal experiment design
  - Design of Experiments

## 2. Probabilistic models

- Guidelines for model building

# Kinetic models

# Kinetic models

**Definition** these models quantify the effect of one or multiple intrinsic or extrinsic factors on the microbial evolution rate

- Inactivation during processing
- Growth during storage

# Kinetic models

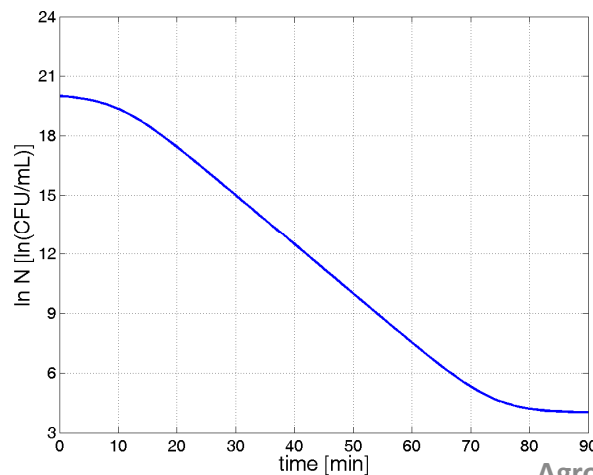
## *Growth & inactivation*

### General expression for microbial evolution

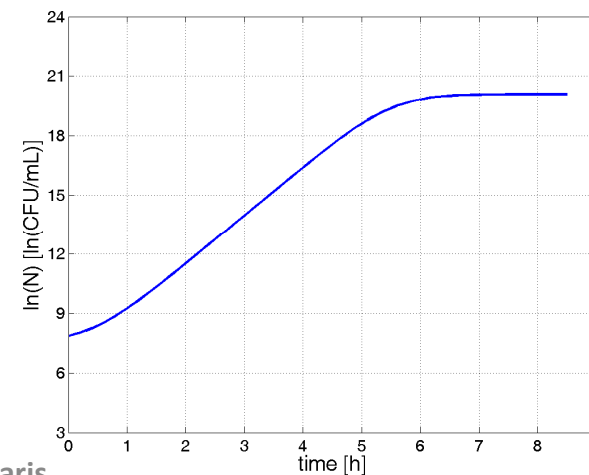
$$\frac{dN(t)}{dt} = \mu \cdot N(t)$$

Primary model

$\mu < 0$



$\mu > 0$

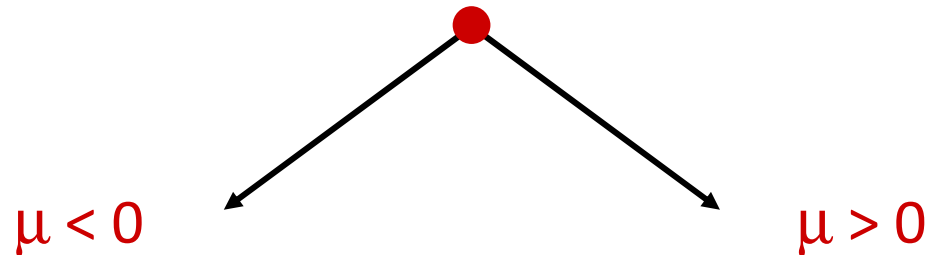


# Kinetic models

## *Growth & inactivation*

### General expression for microbial evolution

$$\frac{dN(t)}{dt} = \mu(< env>, < phys>, S, P, \dots) \cdot N(t)$$



### Secondary model

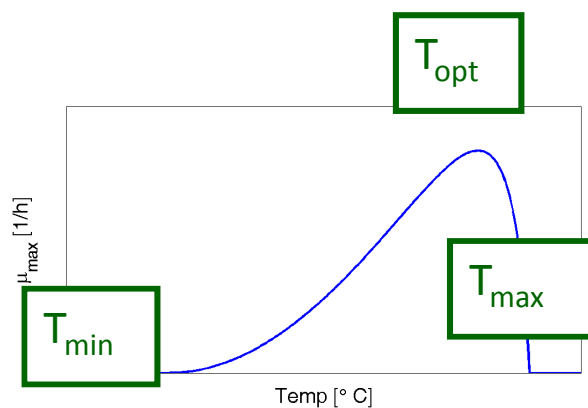
models to describe the effect of the influencing factors as a function of time

# Kinetic growth rate models

## Case study 1. Optimal Experiment Design (OED)

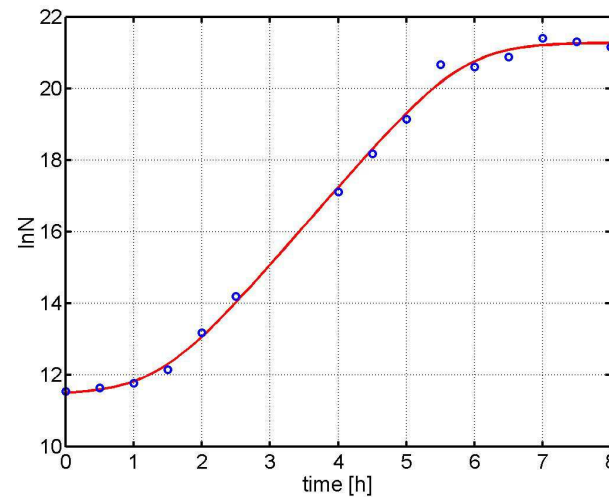
- Parameter estimation
- Model structure selection

### Kinetic model: effect of temperature on $\mu_{\max}$



- Different areas of interest
  - Fermentation processes
  - Soil microbiology: compost processes
  - Microbial food safety

# Microbial dynamics & temperature



## Primary growth model

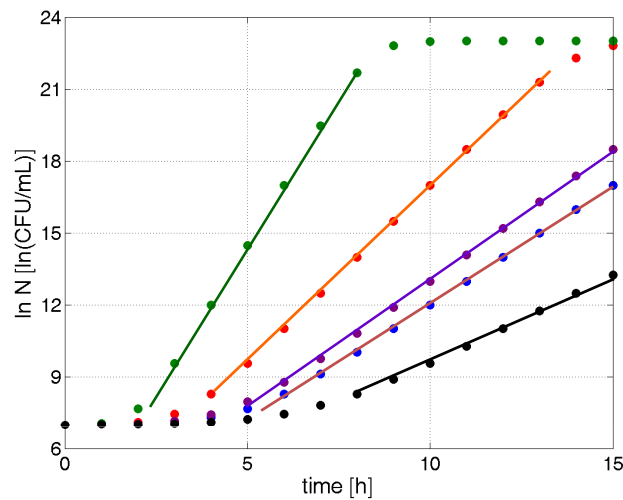
Baranyi and Roberts (1994)

$$\frac{dN(t)}{dt} = \frac{Q(t)}{Q(t) + 1} \cdot \mu_{\max} \cdot \left( 1 - \frac{N(t)}{N_{\max}} \right) \cdot N(t)$$

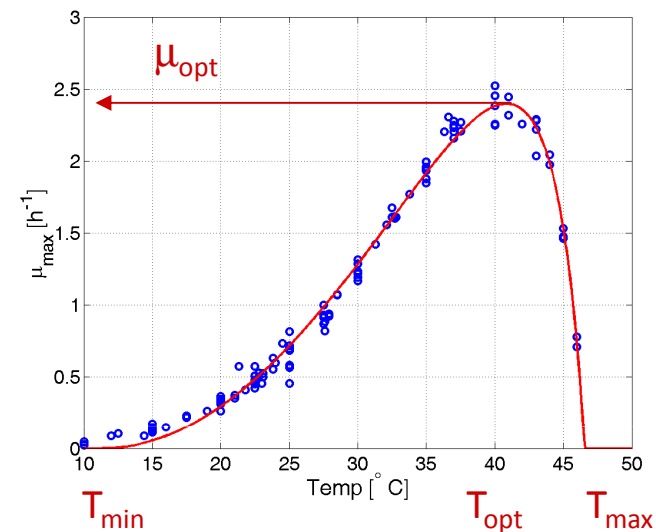
$$\frac{dQ(t)}{dt} = \mu_{\max} \cdot Q(t)$$



# Microbial dynamics & temperature



$\mu_{max}(T)$



## Secondary model

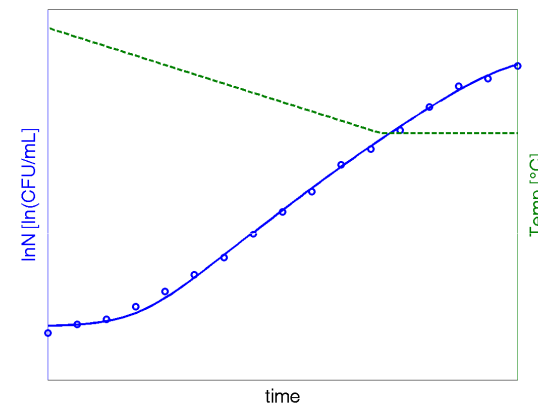
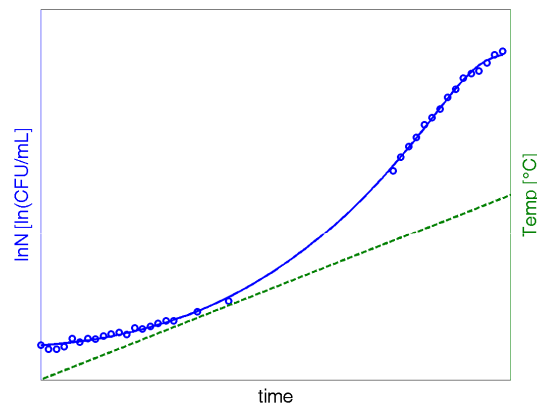
Cardinal temperature model with inflection - CTMI (Rosso et al. 1993)

$$\mu_{max} = \mu_{opt} \cdot \gamma(T)$$

$$\gamma(T) = \frac{(T - T_{min})^2 (T - T_{max})}{(T_{opt} - T_{min})((T_{opt} - T_{min})(T - T_{opt}) - (T_{opt} - T_{max})(T_{opt} + T_{min} - 2T))}$$

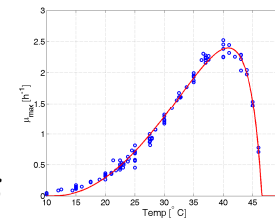
# Microbial dynamics & temperature

Primary growth model & Secondary CTMI model



**Predictive quality** depends on ...

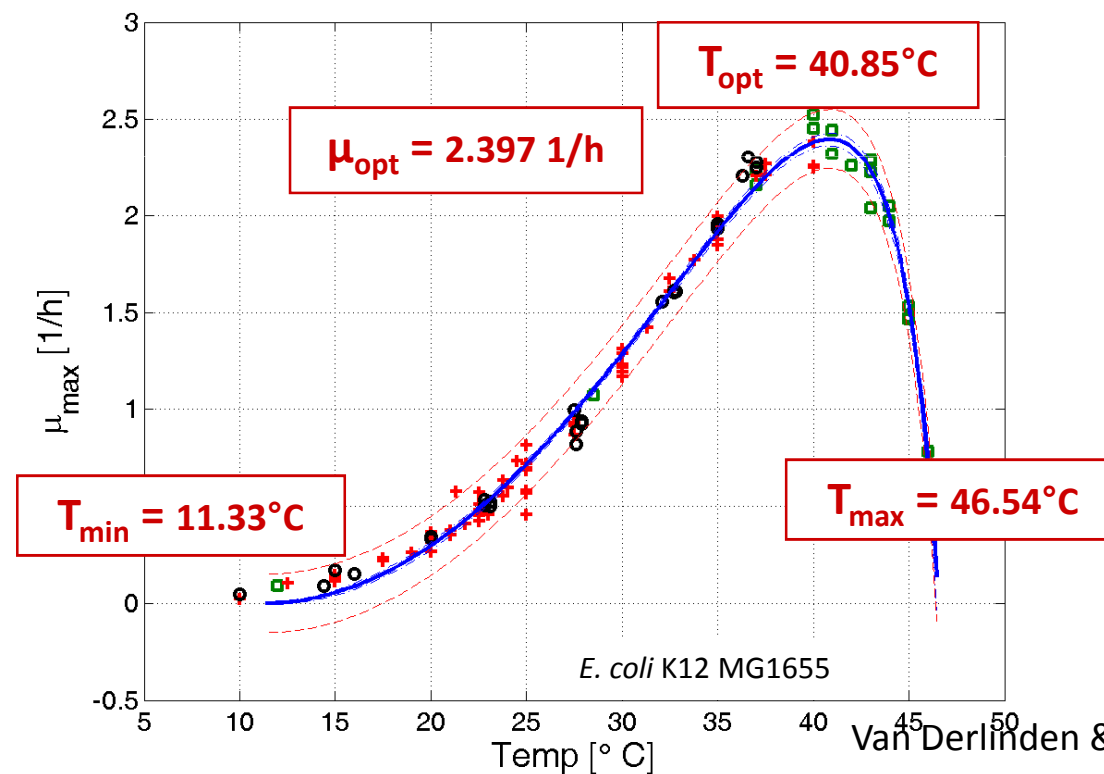
- quality of the *model structure*
- quality of the *model parameter estimates*  
→  $T_{\min}$ ,  $T_{\text{opt}}$ ,  $T_{\max}$  and  $\mu_{\text{opt}}$



# Microbial dynamics & temperature

Efficient and accurate estimation of  
the four CTMI parameters  $T_{\min}$ ,  $T_{\text{opt}}$ ,  $T_{\max}$  &  $\mu_{\text{opt}}$

## 1. Static data collection (= constant T)



Van Derlinden & Van Impe (2012, IJFM)

# Microbial dynamics & temperature

## 2. Dynamic data collection (= dynamic $T(t)$ )

- evaluate model validity under time-varying environmental conditions
- efficient ~ time & labor



selection of dynamic experiments via **OED/PE**

⇒ optimal dynamic temperature profile which maximizes the information content in the experimental data (=  $n(t)$ )

⇒ selection of informative temperature zones: best **p**-estimation



- > reliable and accurate **p** estimates
- > limited set of dynamic experiments

# OED/PE framework

## *Optimization strategy*

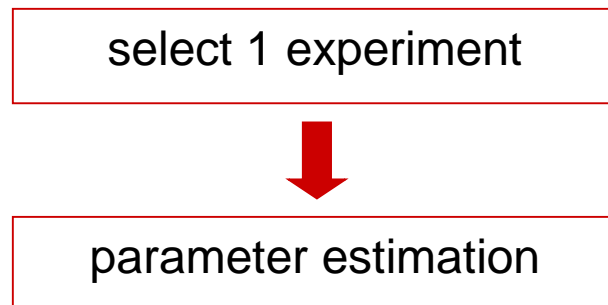
Efficient and accurate estimation of  
the four CTMI parameters  $T_{\min}$ ,  $T_{\text{opt}}$ ,  $T_{\max}$  &  $\mu_{\text{opt}}$   
via  
Optimal Dynamic Experiment Design for  
Parameter Estimation (OED/PE)

- (1) Single OED/PE
- (2) Sequential OED/PE
- (3) Global OED/PE

# OED/PE framework

## *Optimization strategy*

- (1) Single OED/PE
- (2) Sequential OED/PE
- (3) Global OED/PE

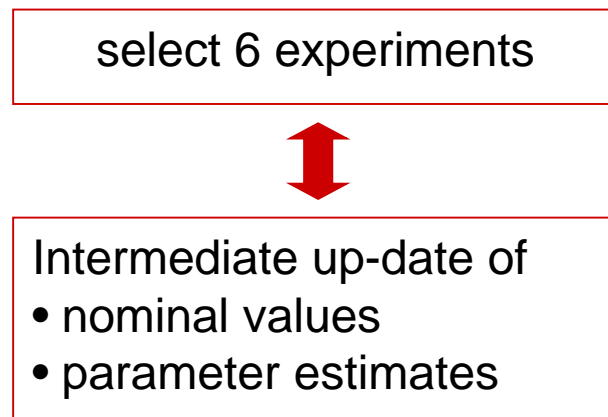


- ? 4  $p_{CTMI}$  from 1 experiment

# OED/PE framework

## Optimization strategy

- (1) Single OED/PE
- (2) Sequential OED/PE  $\Rightarrow$  two-by-two estimation
- (3) Global OED/PE

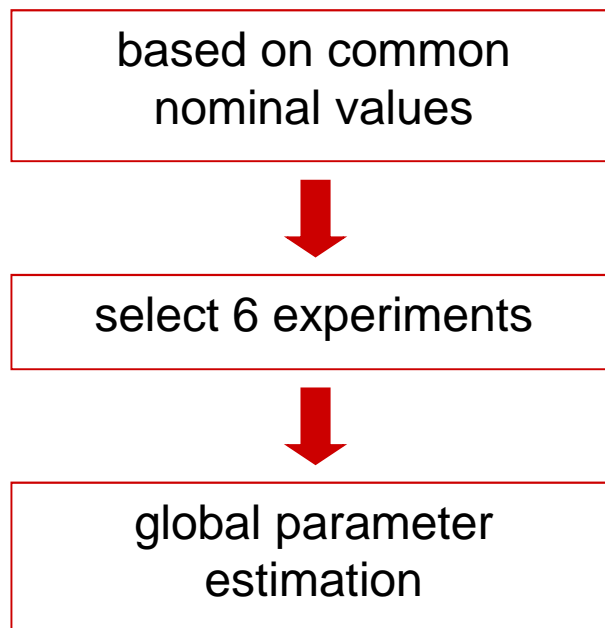


Exp.	considered parameters	nominal parameters
1	$(p_1, p_2)$	$(p_1^0, p_2^0, p_3^0, p_4^0)$
2	$(p_1, p_3)$	$(p_1^1, p_2^1, p_3^0, p_4^0)$
3	$(p_1, p_4)$	$(p_1^2, p_2^1, p_3^1, p_4^0)$
4	$(p_2, p_3)$	$(p_1^3, p_2^1, p_3^1, p_4^1)$
5	$(p_2, p_4)$	$(p_1^3, p_2^2, p_3^2, p_4^1)$
6	$(p_3, p_4)$	$(p_1^3, p_2^3, p_3^2, p_4^2)$

# OED/PE framework

## Optimization strategy

- (1) Single OED/PE
- (2) Sequential OED/PE
- (3) Global OED/PE  $\Rightarrow$  two-by-two estimation



parameters considered	parameters 'known'
$(T_{max}, \mu_{opt})$	$(T_{min}, T_{opt})$
$(T_{max}, T_{min})$	$(T_{opt}, \mu_{opt})$
$(T_{max}, T_{opt})$	$(T_{min}, \mu_{opt})$
$(T_{min}, \mu_{opt})$	$(T_{max}, T_{opt})$
$(T_{min}, T_{opt})$	$(T_{max}, \mu_{opt})$
$(T_{opt}, \mu_{opt})$	$(T_{max}, T_{min})$



# OED/PE framework

## *Fisher information matrix*

**Fisher information matrix:** information quantification

$$\mathbf{F} = \int_0^{t_f} \left( \frac{\partial n(t)}{\partial \mathbf{p}} \right) \Big|_{\mathbf{p}=\mathbf{p}^o} \cdot \mathbf{Q} \cdot \left( \frac{\partial n(t)}{\partial \mathbf{p}} \right)^T \Big|_{\mathbf{p}=\mathbf{p}^o} \cdot dt$$

→ **Dynamic optimization problem**

$$T_{input}(t) = \arg \min / \max [scal(\mathbf{F}(T_{input}(t), \mathbf{p}))]$$

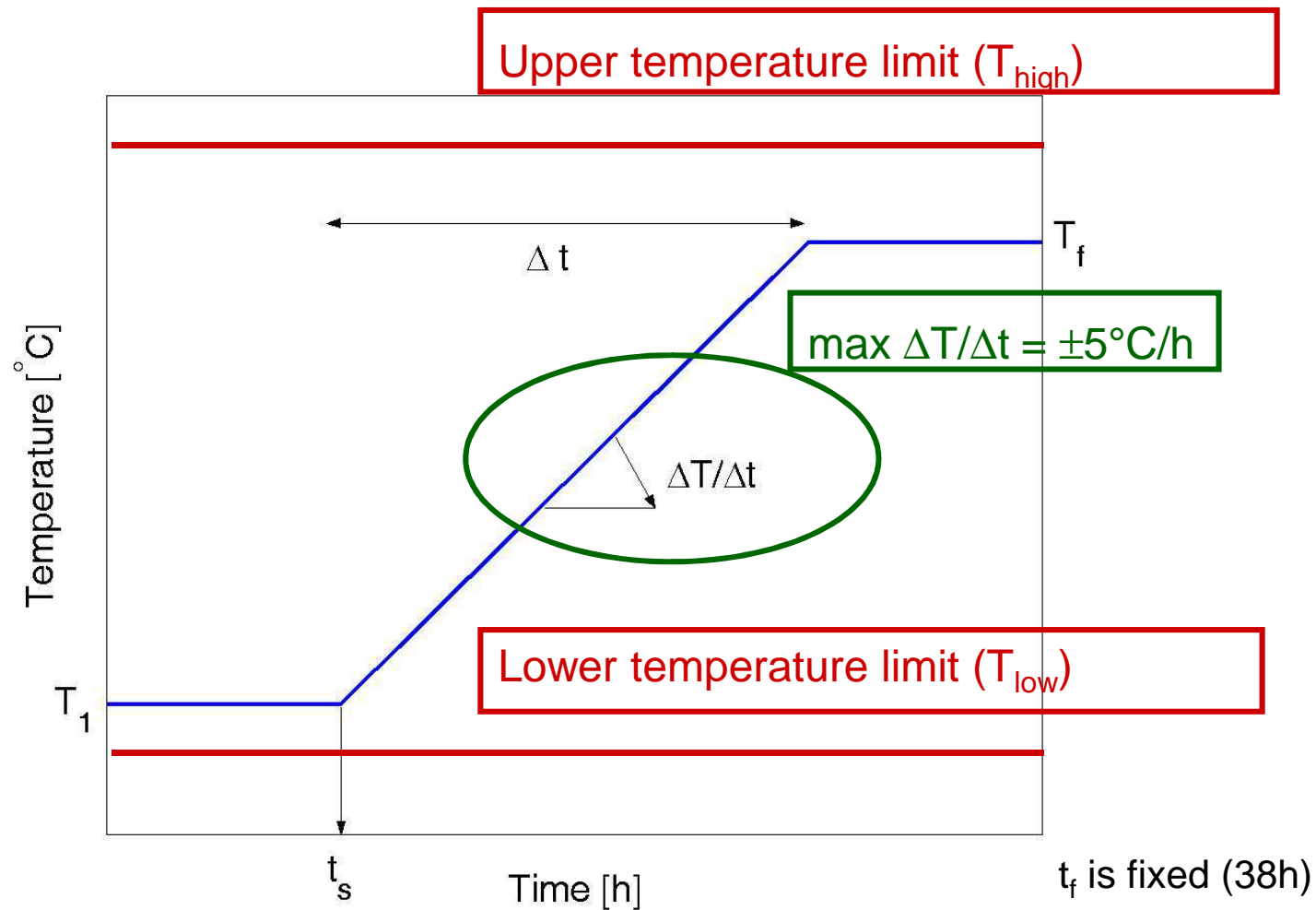
- *Output:*  $n(t) = \ln(N(t))$
- *Parameter vector:*  $\mathbf{p}_{CTMI} = [T_{min} \ T_{opt} \ T_{max} \ \mu_{opt}]^T$
- *Criterion:* D-criterion ( $\max[|\mathbf{F}|]$ )
- *Nominal values:*  $\mathbf{p}^o$

Van Derlinden et al. (2010, JTB)

Telen, Logist, Van Derlinden & Van Impe – Agrostat (2012) On the trade-off between experimental effort and information content in optimal experiment design

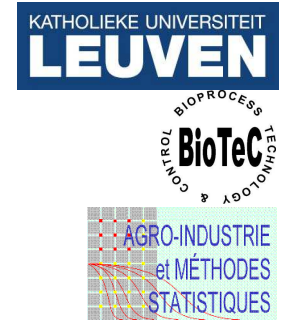
# OED/PE framework

## *Control vector parameterization*



# OED/PE

## *Comparison of three optimization strategies*



### **1. Simulation study**

### **2. Experimental study**

- Bioreactor experiments
- *Escherichia coli* K12

## **PART I.**

### Comparison of three OED/PE strategies via a simulation study

# OED/PE Part I. Simulation study

## *Methodology*

### Three steps

1. Design of D-optimal experiments
2. Simulation of growth curves
  - based on the true parameters
  - error ~ measurement error and biological variability
3. Estimation of parameters from simulated experimental data
  - minimization of the sum of squared errors

- three different sets of true parameters ( $\mathbf{p}^*$ )
- **SiOED/PE & GIOED/PE** → identical nominal parameters
- **SeOED/PE** → different order of  $\mathbf{p}$ -combinations

# OED/PE Part I. Simulation study

## Results

(Initial) nominal values

$$T_{\min}^{\circ} = 11.33$$

$$T_{\max}^{\circ} = 46.54$$

$$T_{\text{opt}}^{\circ} = 40.85$$

$$\mu_{\text{opt}}^{\circ} = 2.396$$

Van Derlinden et al. (2010, JTB)

## Results

	p*	SiOED/PE	SeOED/PE	GIOED/PE
$T_{\min}$	8.000	8.073 ( $4.371 \times 10^{-1}$ )	6.163 ( $1.852 \times 10^{-1}$ )	7.822 ( $1.072 \times 10^{-1}$ )
$T_{\text{opt}}$	40.00	40.10 ( $5.288 \times 10^{-1}$ )	40.84 ( $1.241 \times 10^{-1}$ )	40.12 ( $7.278 \times 10^{-2}$ )
$T_{\max}$	46.00	46.17 ( $4.112 \times 10^{-1}$ )	45.51 ( $3.278 \times 10^{-2}$ )	45.92 ( $3.549 \times 10^{-4}$ )
$\mu_{\text{opt}}$	2.200	2.184 ( $7.795 \times 10^{-2}$ )	2.368 ( $2.305 \times 10^{-2}$ )	2.204 ( $1.110 \times 10^{-2}$ )
$T_{\min}$	6.500	6.464 ( $4.385 \times 10^{-1}$ )	4.256 ( $5.445 \times 10^{-1}$ )	6.491 ( $1.146 \times 10^{-1}$ )
$T_{\text{opt}}$	39.80	40.00 ( $5.601 \times 10^{-1}$ )	42.04 ( $6.403 \times 10^{-2}$ )	40.09 ( $8.706 \times 10^{-2}$ )
$T_{\max}$	45.70	45.78 ( $2.184 \times 10^{-1}$ )	45.19 ( $1.012 \times 10^{-4}$ )	45.55 ( $2.437 \times 10^{-5}$ )
$\mu_{\text{opt}}$	2.000	2.007 ( $5.656 \times 10^{-2}$ )	2.173 ( $1.698 \times 10^{-2}$ )	2.051 ( $1.246 \times 10^{-2}$ )
$T_{\min}$	10.00	10.08 ( $3.683 \times 10^{-1}$ )	9.828 ( $2.779 \times 10^{-1}$ )	9.889 ( $8.118 \times 10^{-2}$ )
$T_{\text{opt}}$	40.50	40.47 ( $5.744 \times 10^{-1}$ )	40.61 ( $1.123 \times 10^{-1}$ )	40.58 ( $1.576 \times 10^{-1}$ )
$T_{\max}$	45.30	45.40 ( $1.635 \times 10^{-1}$ )	45.27 ( $1.063 \times 10^{-2}$ )	45.29 ( $3.415 \times 10^{-2}$ )
$\mu_{\text{opt}}$	2.350	2.318 ( $9.301 \times 10^{-2}$ )	2.392 ( $7.863 \times 10^{-2}$ )	2.348 ( $2.823 \times 10^{-2}$ )

## PART II.

Comparison of SiOED/PE and GIOED/PE strategies based  
on experimental data

# OED/PE Part II. Experiments

## Experimental set-up

Optimal experiment design for  
parameter estimation



- *Escherichia coli*

Experimental implementation



cell density  
plate counting

microorganism is grown in  
laboratory medium

measurements & control

T, pH, aeration & dissolved oxygen, rpm



# OED/PE Part II. *Escherichia coli*

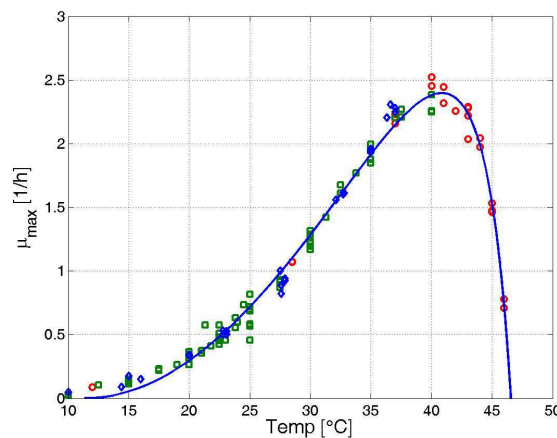
## Background

✓ T effect on *E. coli* dynamics  
extensively studied @ KULeuven/BioTeC

- Swinnen et al. (2005, 2006)
- Bernaerts et al. (2000, 2002)
- Valdramidis et al. (2006, 2007)

✓ advantage

- design of constraints
- selection of realistic nominal values



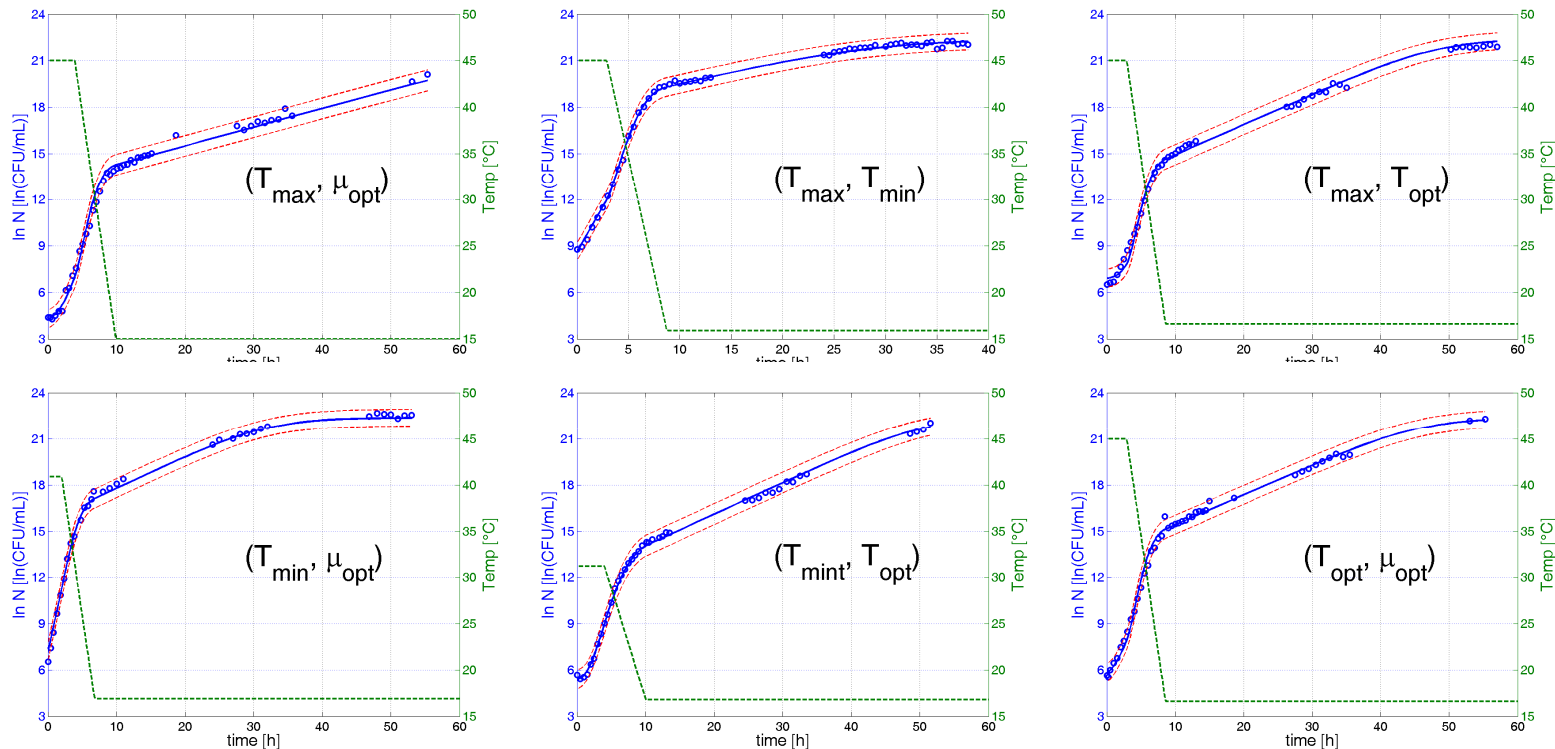
### Nominal values

- $T_{min}$  = 11.33°C
- $T_{opt}$  = 40.85°C
- $T_{max}$  = 46.54°C
- $\mu_{opt}$  = 2.397°C

✓  $(\Delta T/\Delta t)_{max} = 5^\circ\text{C/h}$ ,  $t_f = 38\text{h}$

# OED/PE Part II. *Escherichia coli*

## Results – Global strategy (GLOED/PE)

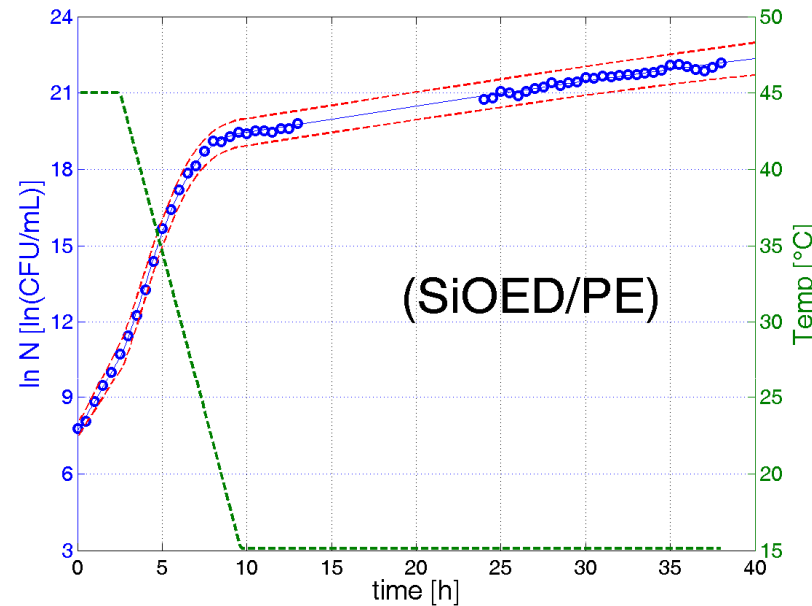


- Reliable estimates for  $T_{\min}$ ,  $T_{\text{opt}}$ ,  $T_{\max}$  and  $\mu_{\text{opt}}$
- Similar to values obtained from static experiments
- Low uncertainty

Van Derlinden et al. (2010, JTB)

# OED/PE Part II. *Escherichia coli*

## Results – Single strategy (SiOED/PE)



Van Derlinden et al. (2010, JTB)

- Reliable and accurate CTMI parameter estimates

# OED/PE

## *General conclusions*

### Three optimization strategies

- SiOED/PE
- SeOED/PE
- GIOED/PE

#### 1) simulation study

→ SeOED/PE repeatedly in unrealistic  $p_{CTMI}$  estimates

#### 2) reliable and accurate CTMI parameter estimates derived from the six GIOED/PE optimal experiments

→ each CTMI parameter is considered three times

#### 3) accurate $p_{CTMI}$ estimation not guaranteed via SiOED/PE

→ Information is limited

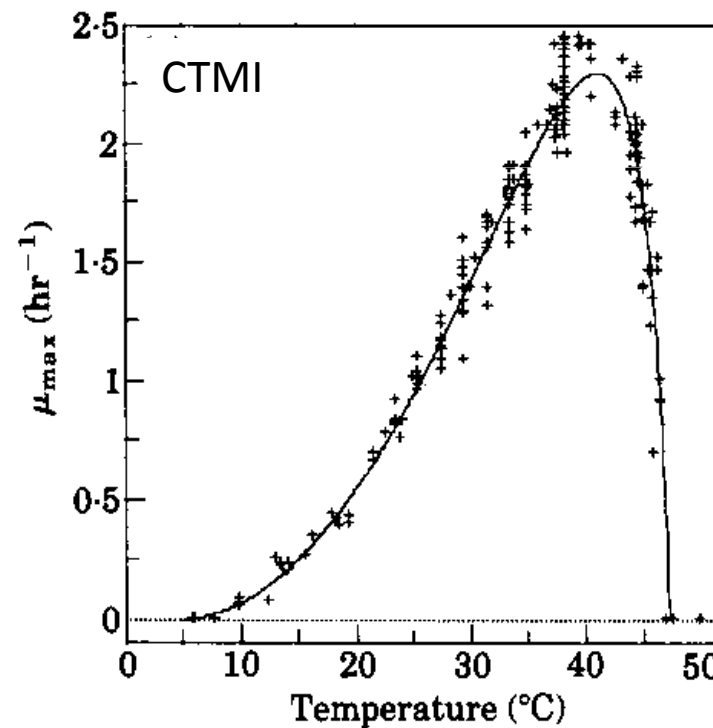
→ Parameter only considered once

29/03/2012 → Highly sensitive to experimental errors

# Microbial dynamics & temperature

## *Multiple model structures*

- Multiple models exist to describe effect of T on  $\mu_{\max}$ 
  - Cardinal Temperature Model with Inflection

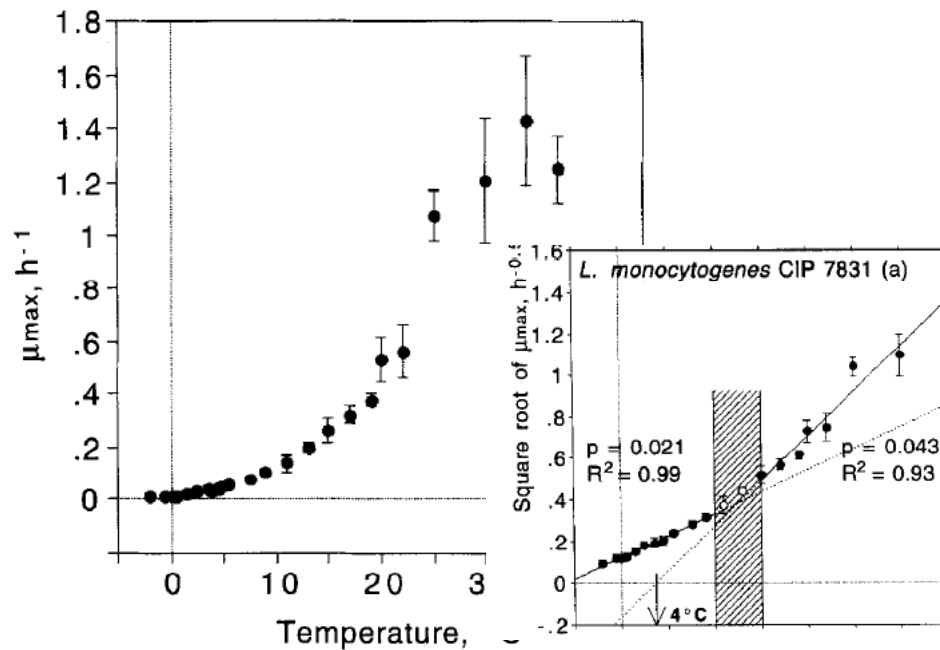


Rosso et al. (1993, JTB)

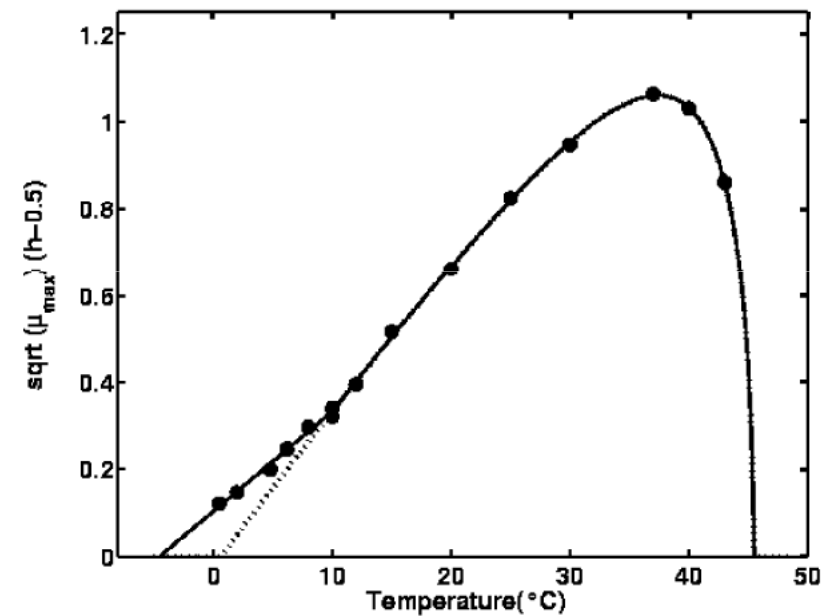
# OED/MD

## Microbial dynamics & temperature

- Deviating behavior observed for *Listeria*



*Listeria monocytogenes* (Bajard et al. 1996, IJFM)



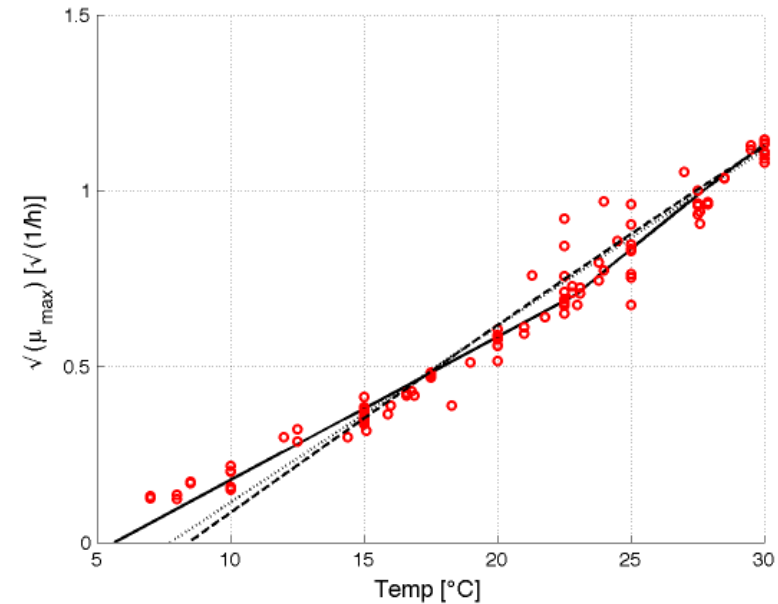
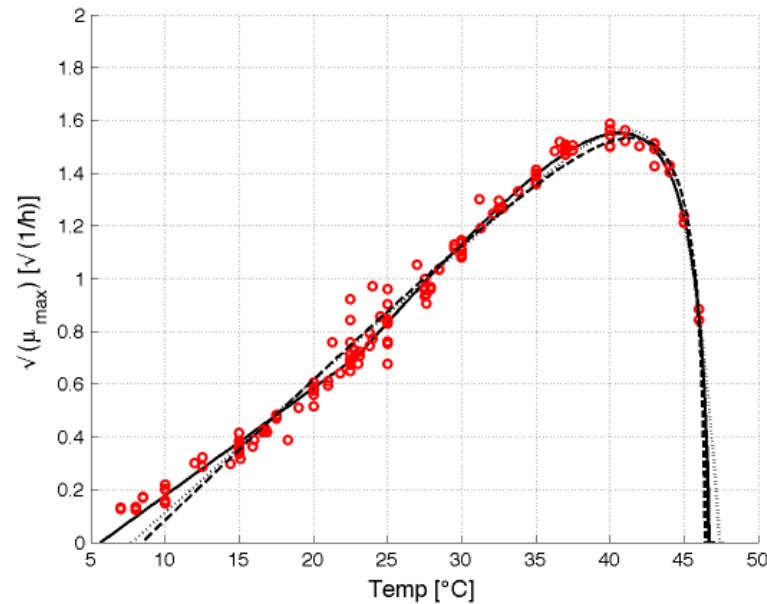
*Listeria innocua* (Le Marc et al. 2002, IJFM)

=> Adapted CTMI model structure by Le Marc et al. (2002, IJFM)

# OED/MD

## *Microbial dynamics & temperature*

- Deviating behavior possible also valid for other strains
- *Escherichia coli* K12



Van Derlinden & Van Impe (2012, IJFM)

# OED/MD

*Microbial dynamics & temperature*

## Work in progress

question: what is the correct model?

## **optimal experiment design for model structure discrimination**

- **Aim** =
  - to design a (set of) dynamic temperature experiments that shows the maximum difference in model output
  - identify which models corresponds most with reality



# Kinetic growth rate models

## Case study 2. Design Of Experiments (DOE)

- Parameter estimation

Kinetic model: effect of temperature, pH, lactic acid and  $a_w$  on  $\mu_{\max}$

# Design Of Experiments

**Design of experiments** includes different - statistically inspired - approaches that result in the structured collection of information with respect to one or more variables, their variability and interactions.

- Identify variables that mainly control the studied system
  - How these variables interact.
- the basic idea behind DOE is to hold certain factors constant and to alter the levels of one or more other variables.

# Design Of Experiments

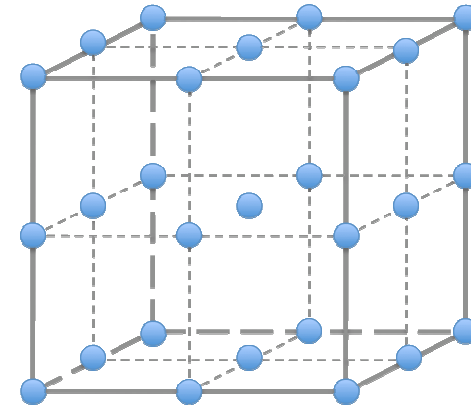
## *Implementations in predictive microbiology*

1. To **scan an extended region**.
  - Probabilistic model building; quantify the chance of survival and/or growth of pathogens or spoilage microorganisms given certain processing conditions  
(Belletti et al., 2007; Gao et al., 2006; Uljas et al., 2001).
1. Extended data collection to build **response surface models**.
  - via polynomial regression,
  - effect of intrinsic/extrinsic factors on selected variables describing microbial dynamics  
(inactivation parameters - Maks et al., 2010).
1. Accurate and reliable parameter **estimates of existing models**.  
(Jagannath et al., 2005; Miller et al., 2009).

# Design Of Experiments

## *Design schemes*

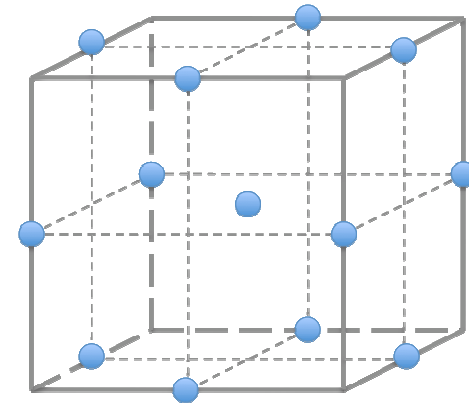
- Experimental design schemes
  - *Full Factorial*
  - Fractional factorial



# Design Of Experiments

## *Design schemes*

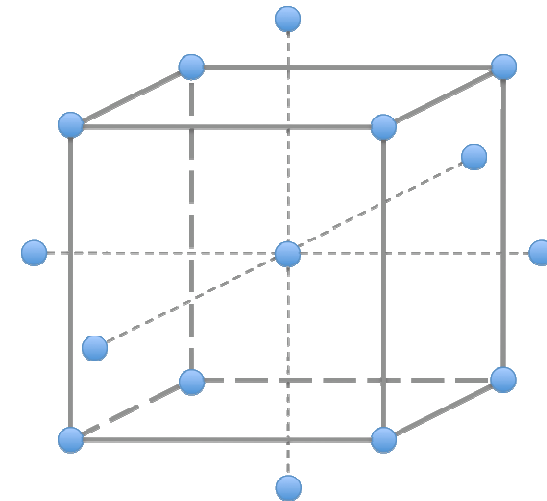
- Experimental design schemes
  - Full Factorial
  - Fractional factorial
  - *Box Behnken*



# Design Of Experiments

## *Design schemes*

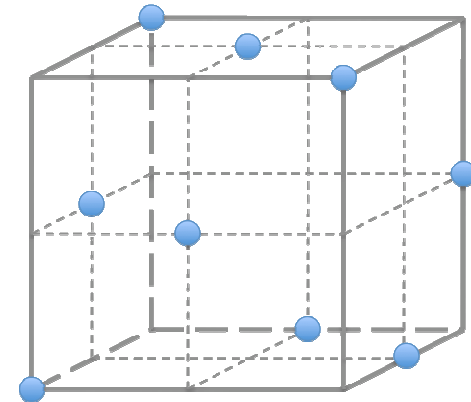
- Experimental design schemes
  - Full Factorial
  - Fractional factorial
  - Box Behnken
  - *Central Composite*



# Design Of Experiments

## *Design schemes*

- Experimental design schemes
  - Full Factorial
  - Fractional factorial
  - Box Behnken
  - Central Composite
  - *Latin Square*



# Case study

## *Research objective*

*Assess the performance of experimental design schemes with respect to parameter estimation of a secondary model*

### Effect on microbial growth rate (*Escherichia coli*)

- Water activity
- Temperature
- pH
- Lactic acid

$$\sqrt{\mu_{\max}} = c \cdot (T - T_{\min}) \cdot (1 - \exp(d(T - T_{\max}))) \cdot \sqrt{a_w - a_{wmin}} \cdot \sqrt{1 - 10^{pH_{\min} - pH}} \cdot \sqrt{1 - 10^{pH - pH_{\max}}} \cdot \sqrt{1 - \frac{LAC}{U_{\min} \cdot (1 + 10^{pH - pK_a})}} \cdot \sqrt{1 - \frac{LAC}{D_{\min} \cdot (1 + 10^{pK_a - pH})}}$$

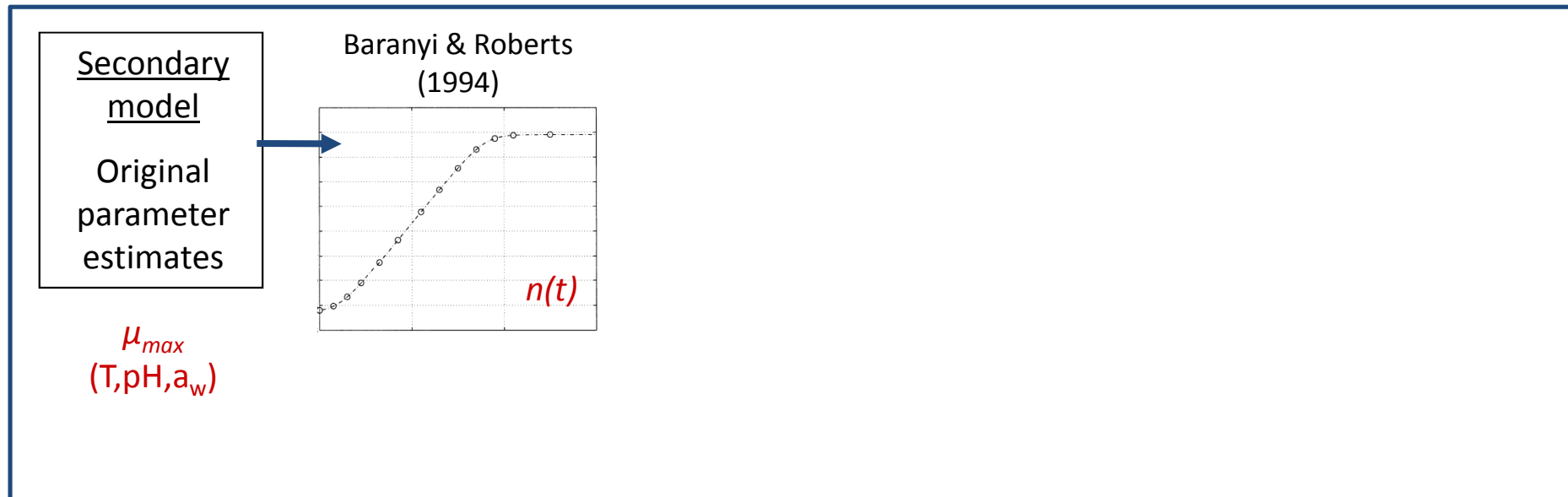
Ross et al. (2002)



# Case study

## *Simulation study*

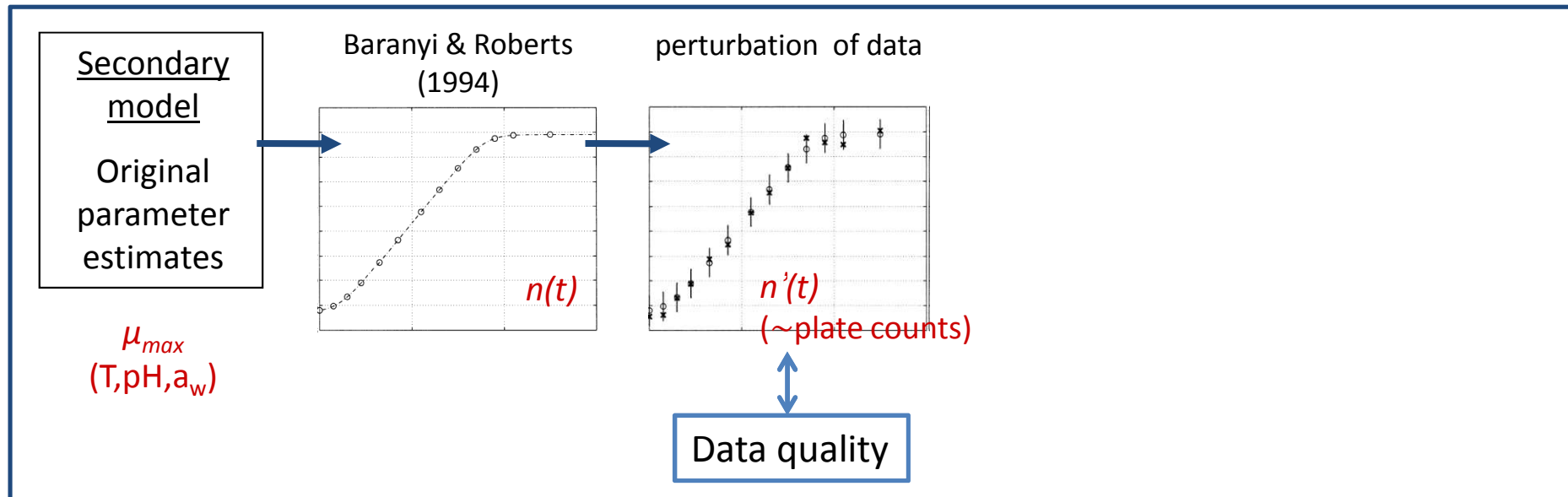
- **Stepwise procedure**



# Case study

## *Simulation study*

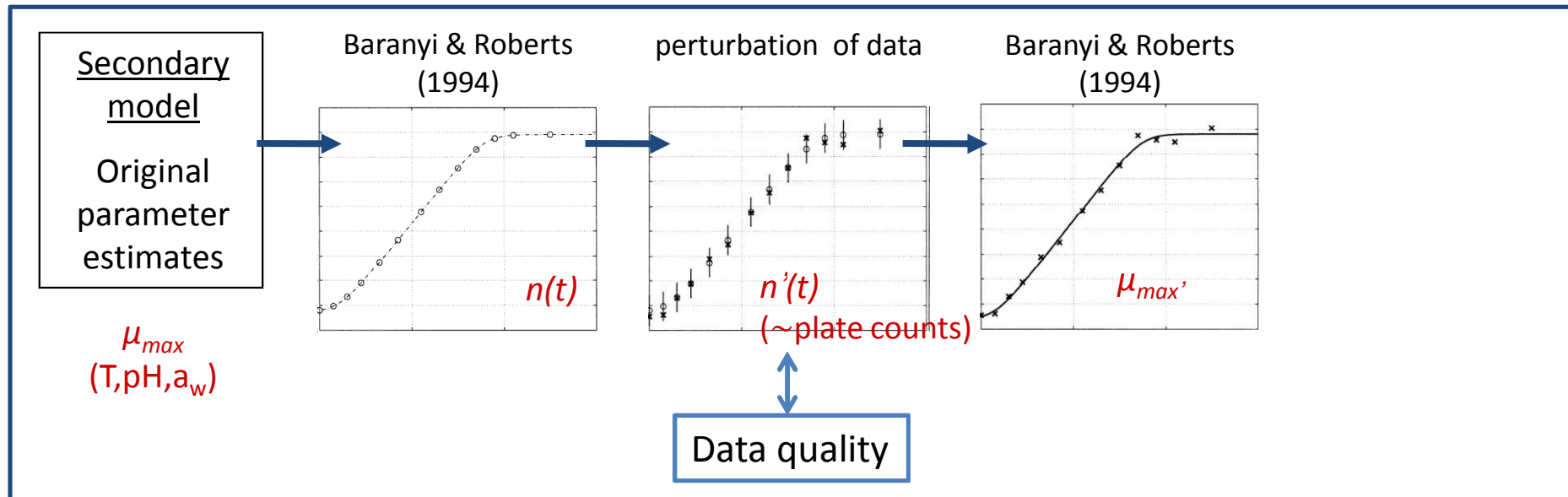
- Stepwise procedure



# Case study

## *Simulation study*

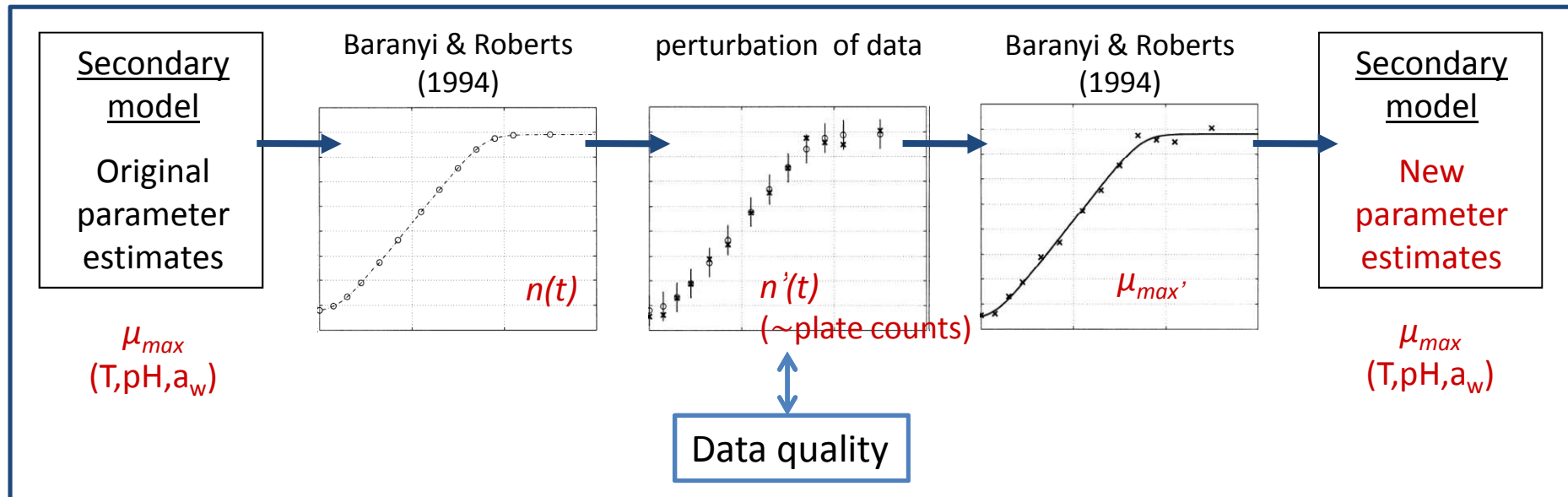
- Stepwise procedure



# Case study

## Simulation study

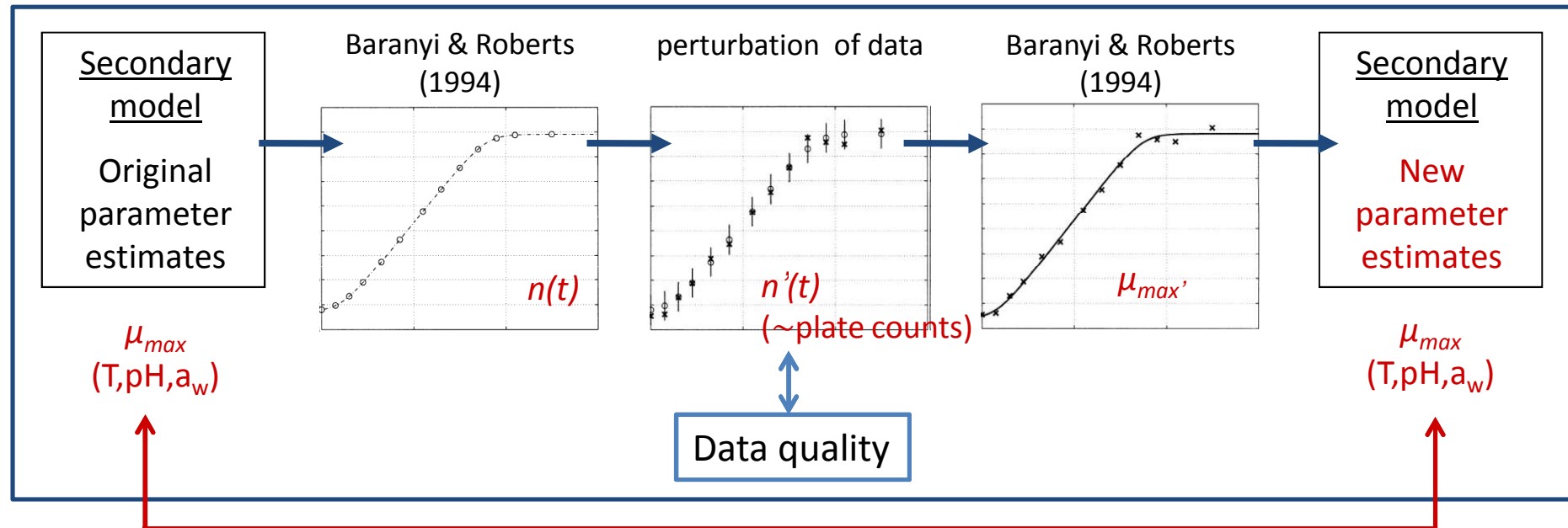
- Stepwise procedure



# Case study

## *Simulation study*

- Stepwise procedure**



### Performance criteria

- # experiments
- goodness-of-fit statistics
- reliability of parameter estimates

# DOE Simulation study

## Overview designs

Design scheme	# levels per factor	# experiments	RMSE
FF5 Full Factorial	5	625	0.009/0.030
RFF Reduced Full Factorial	5*	90	0.009/0.029
LS9 Latin-Square	9	81	0.010/0.029
CC Central Composite	5	36	0.010/0.034
LS5 Latin-Square	5	25	0.008/0.031

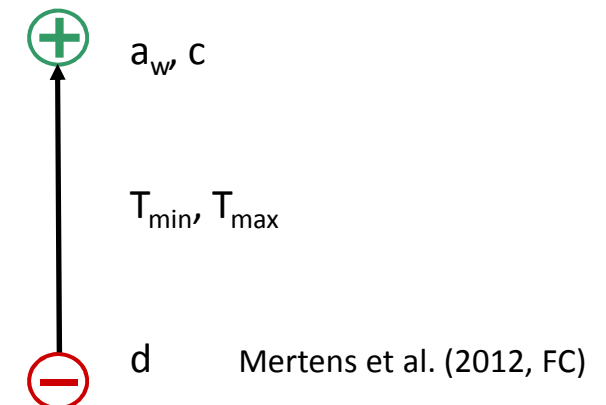
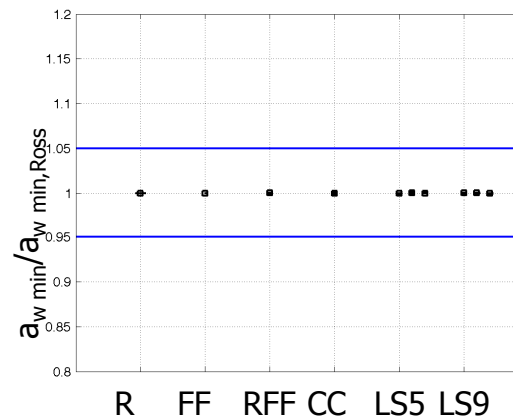
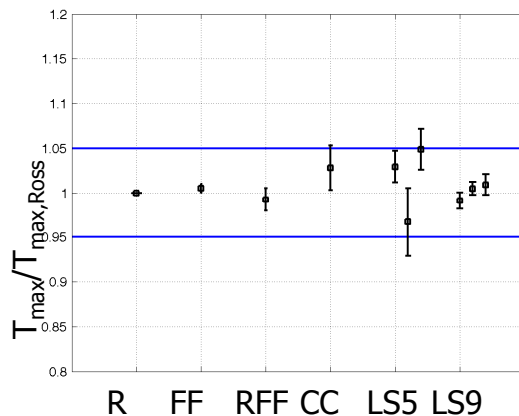
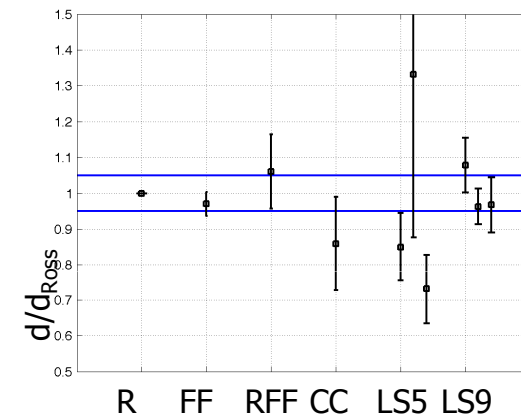
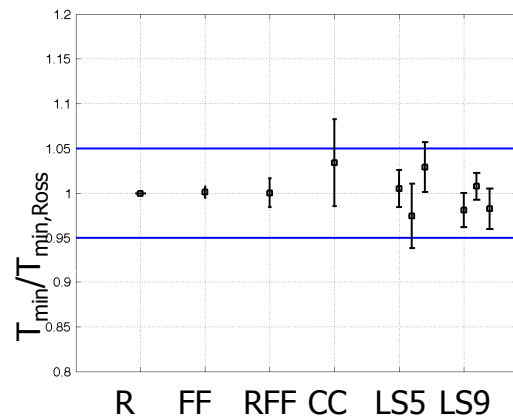
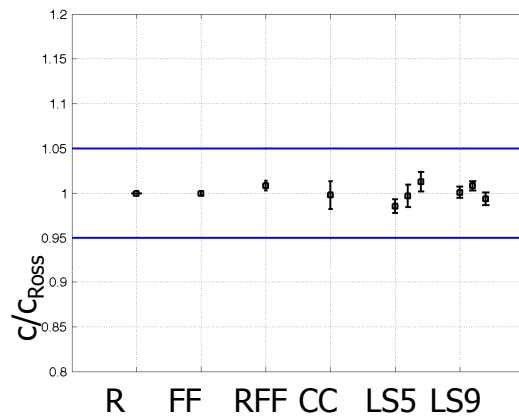
RFF = 5 T, 3 pH, 3 LAC, 2  $a_w$

# DOE Simulation study

## Model parameter estimation results

- Low level of noise on data

$$\sqrt{\mu_{\max}} = c \cdot (T - T_{\min}) \cdot (1 - \exp(d(T - T_{\max}))) \cdot \sqrt{a_w - a_{w\min}} \cdot \sqrt{1 - 10^{pH_{\min} - pH}} \cdot \sqrt{1 - 10^{pH - pH_{\max}}} \cdot \sqrt{1 - \frac{LAC}{U_{\min} \cdot (1 + 10^{pH - pK_a})}} \cdot \sqrt{1 - \frac{LAC}{D_{\min} \cdot (1 + 10^{pK_a - pH})}}$$

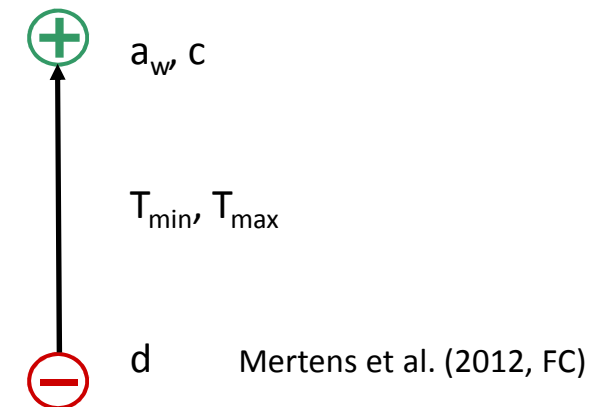
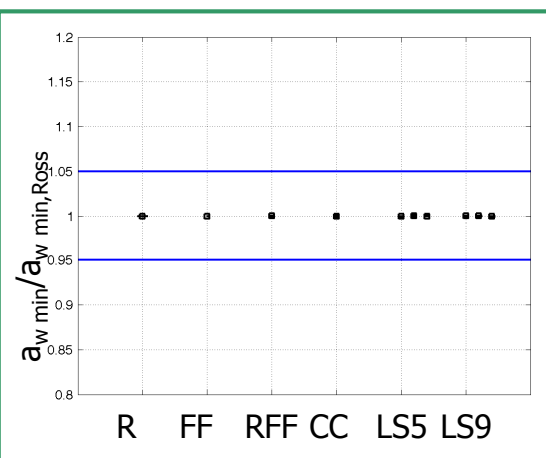
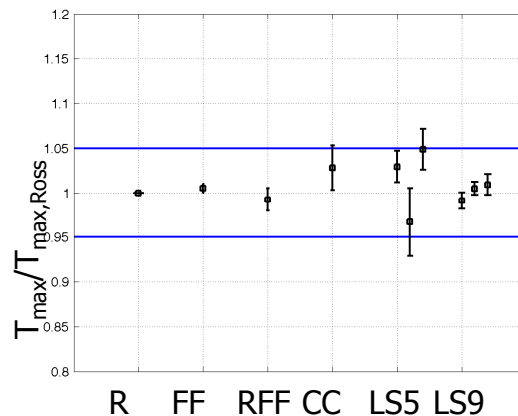
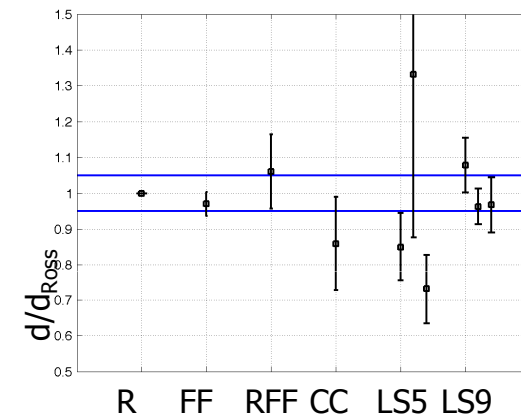
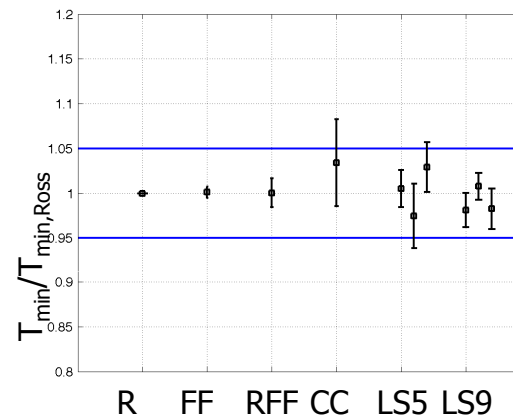
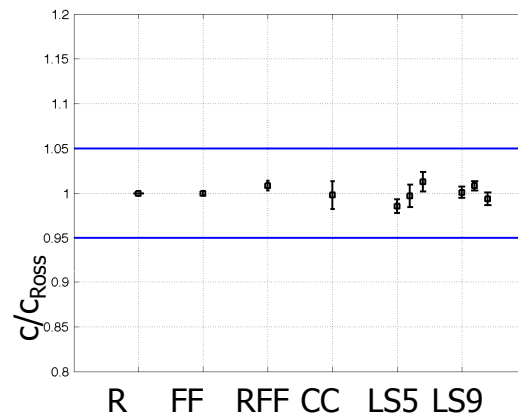


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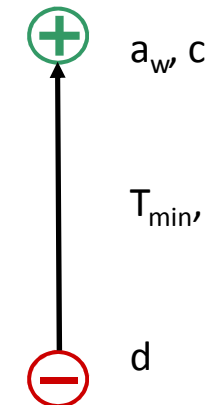
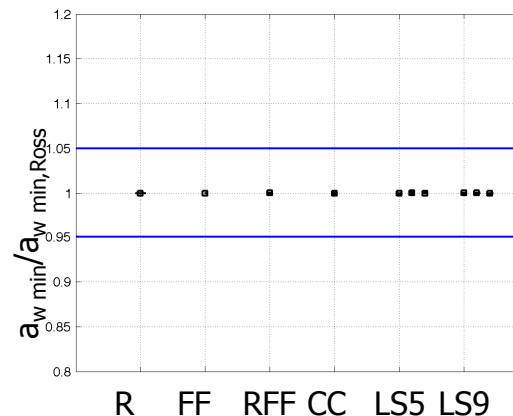
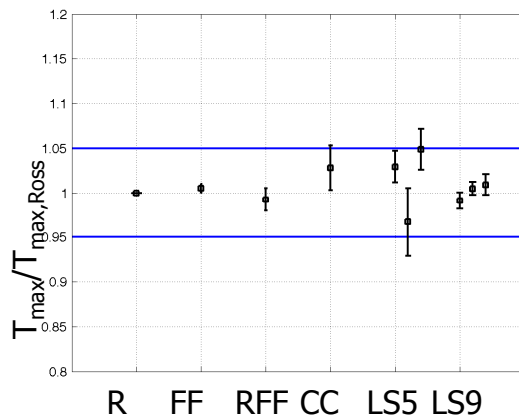
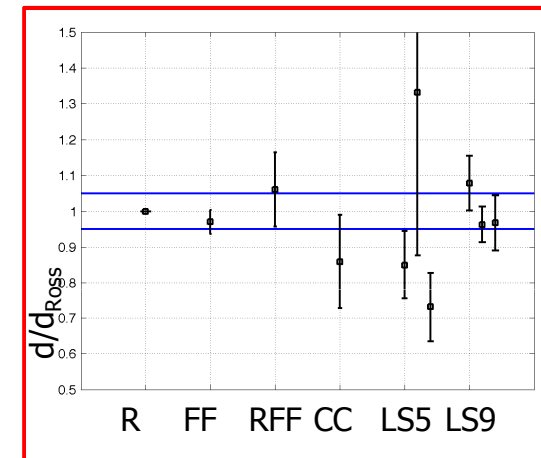
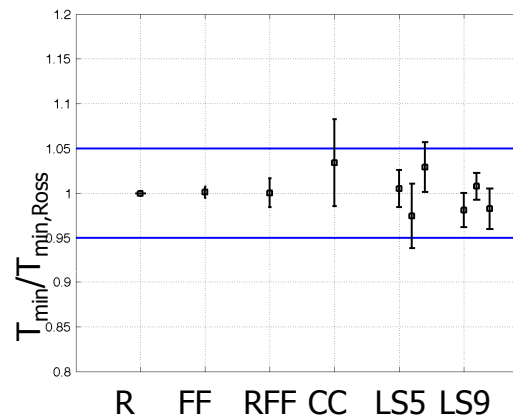
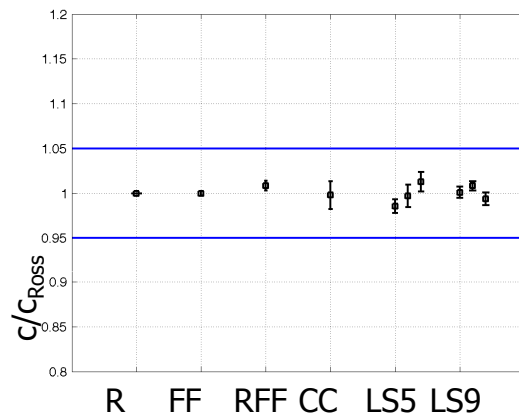


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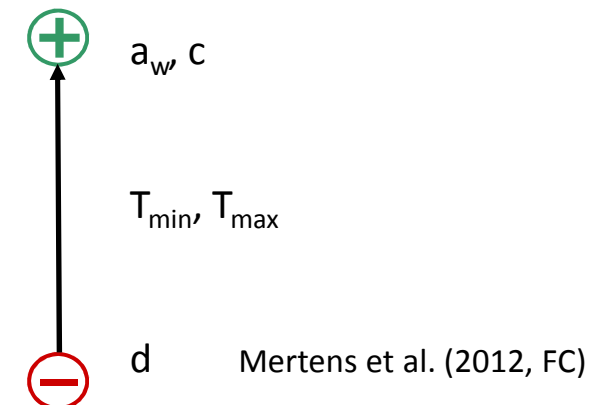
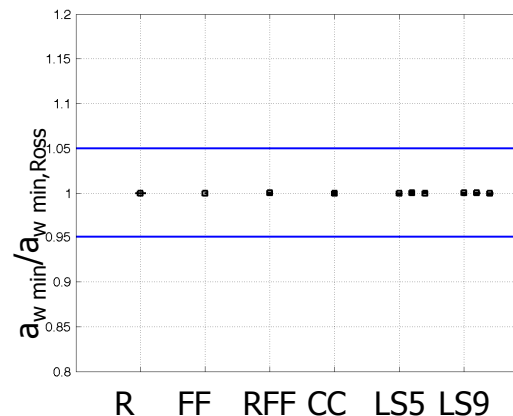
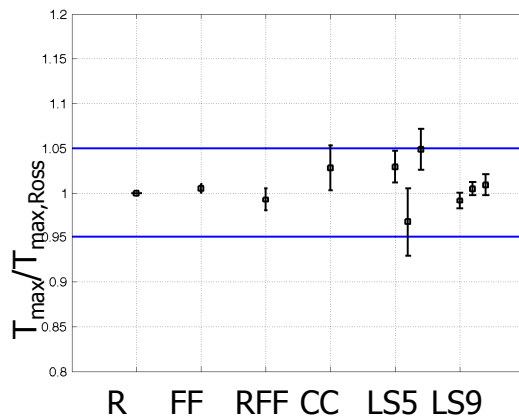
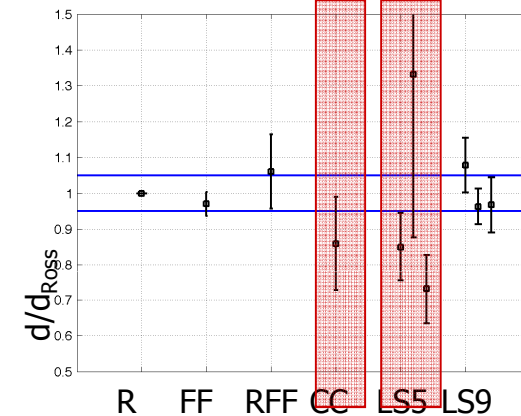
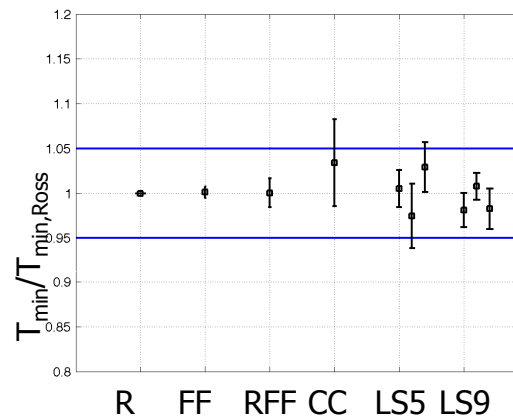
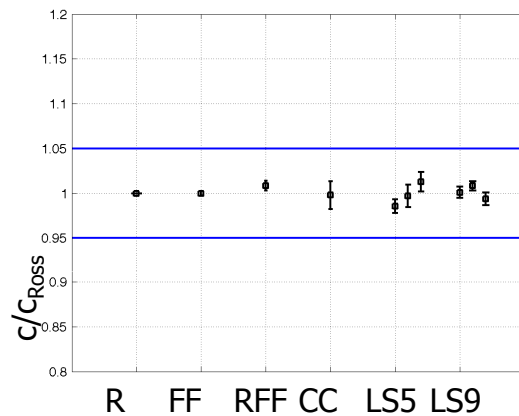
Mertens et al. (2012, FC)

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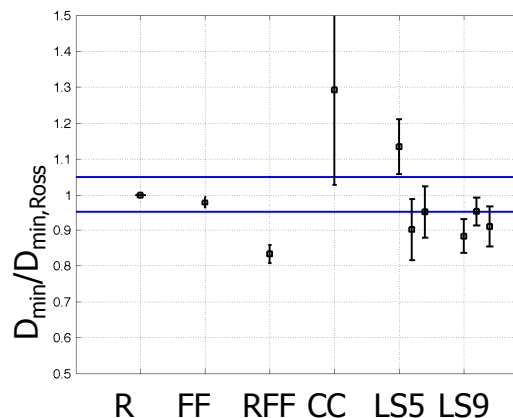
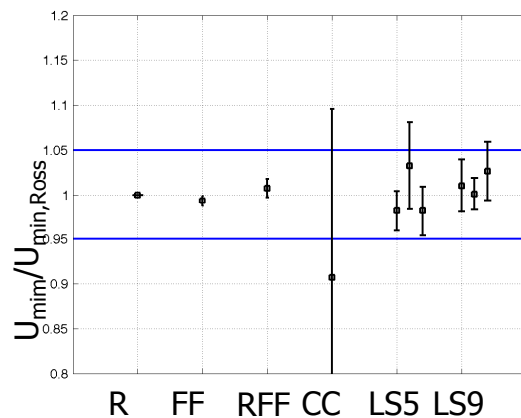
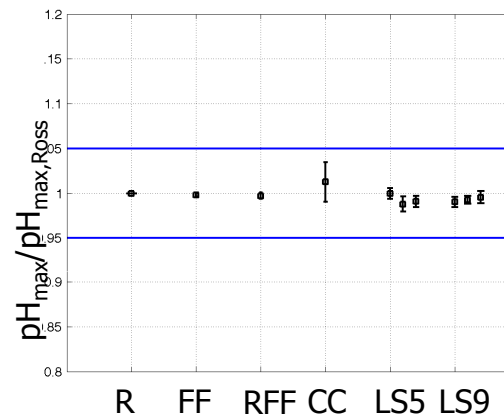
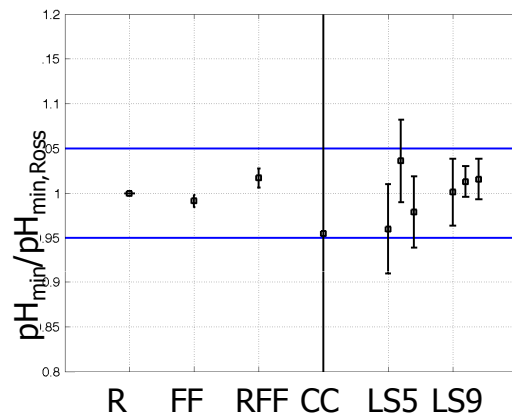


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$pH_{\max}$

$pH_{\min}, U_{\min}$



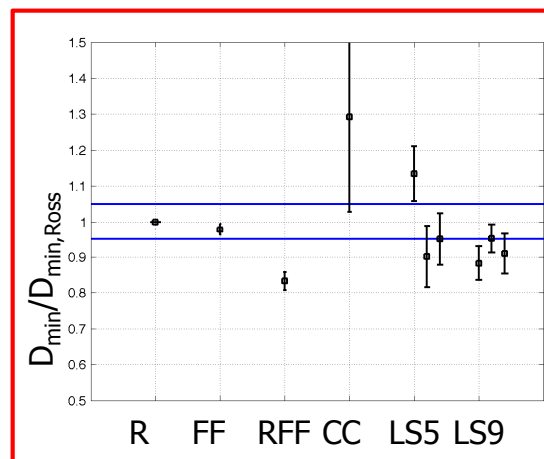
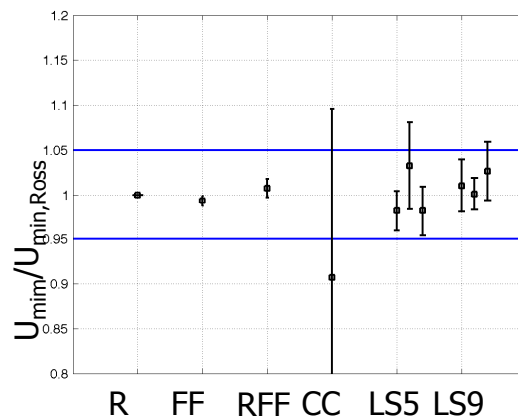
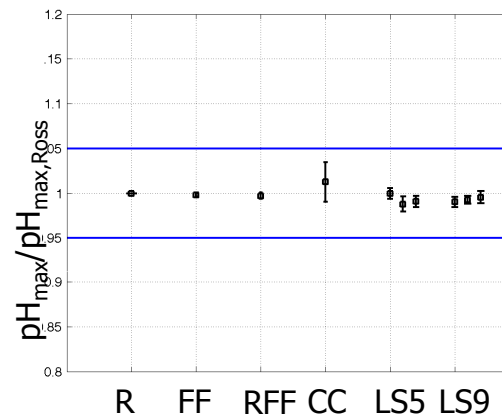
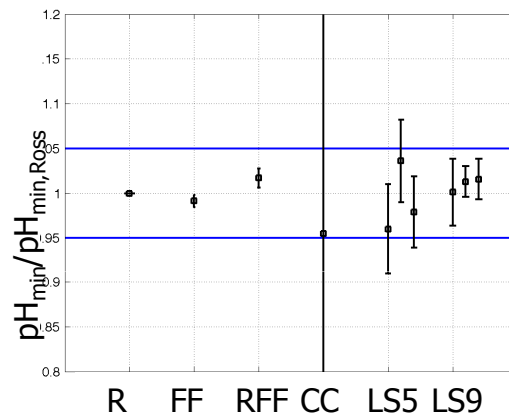
$D_{\min}$  Mertens et al. (2012, FC)

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$pH_{\max}$

$pH_{\min}, U_{\min}$



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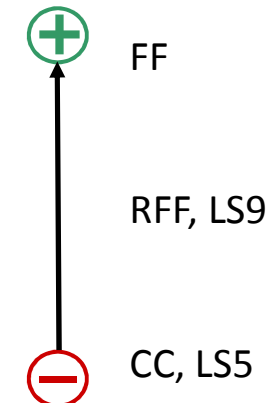
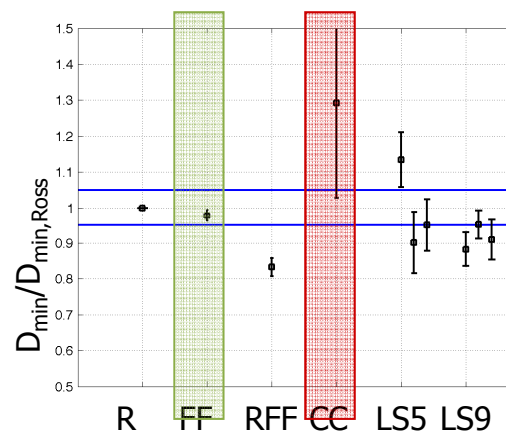
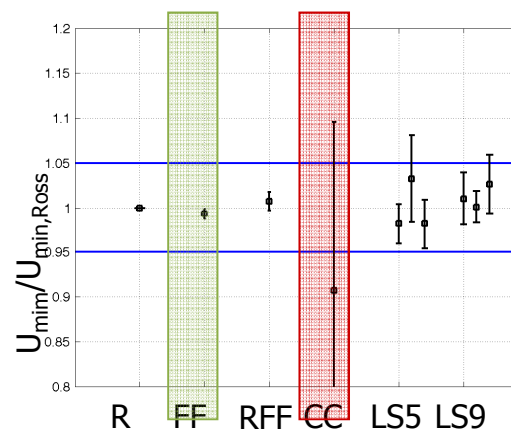
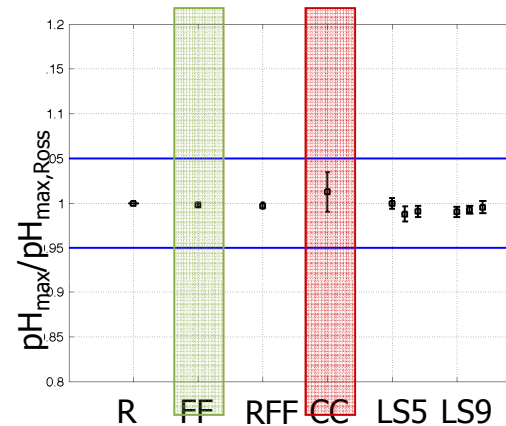
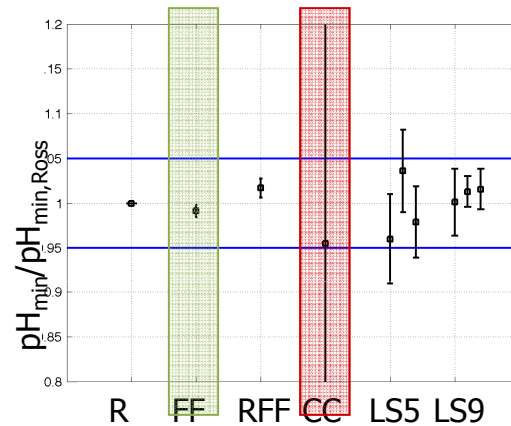
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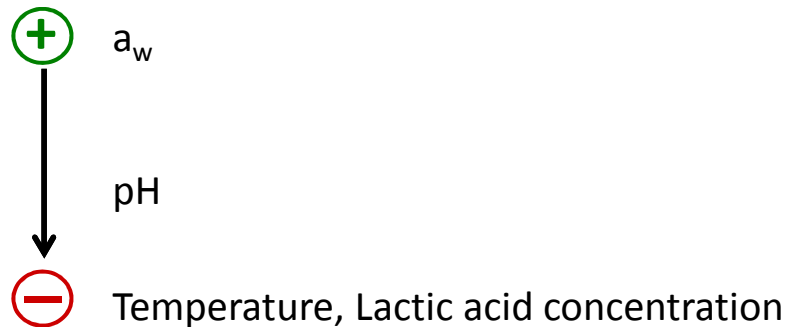
Mertens et al. (2012, FC)



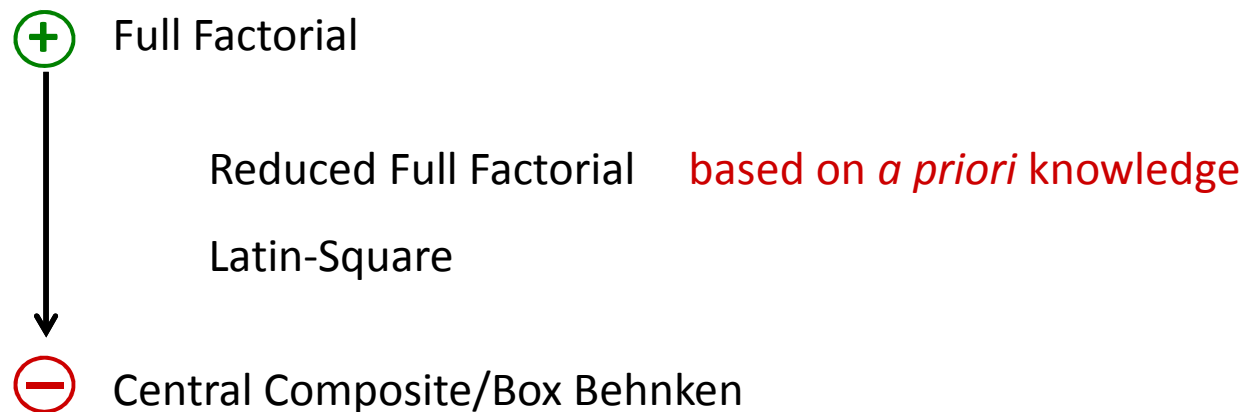
# DOE Simulation study

## Conclusions

*Accuracy & uncertainty of parameter estimates*



*Selecting a design = **trade-off** (data quantity, # levels & factors)*



# Probabilistic models

# Probabilistic models

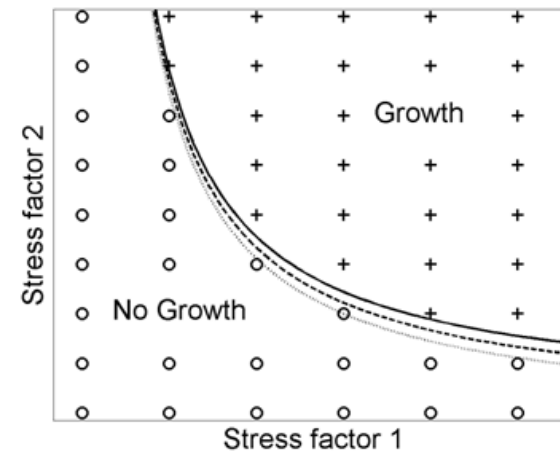
**Definition:** describe the chance that a certain event (growth, survival, toxin production) occurs in a time span given the intrinsic and extrinsic factors.

- a logic continuation of the kinetic growth model
- @ harsher environmental conditions:
  - growth rate is decreasing until zero and
  - lag phase is increasing until eternity
- the boundary between growth and no growth has been reached
- a kinetic model => a probabilistic model
- model output = chance that a certain event will take place within a certain given time



# Probabilistic models

- Responses, under the defined experimental conditions and in a certain period of time, will be coded
  - as either 0 (response not observed)
  - or 1 (response observed).
- Repeated observations @ identical conditions
  - a probability: 0 and 100%



# Probabilistic models

## *Applications in food processing*

- In relation to the (food) composition
  - G/NG models for **pathogens**
    - Low infection dose
    - Growth ability > growth rate
  - G/NG models for **food spoilage** microorganisms
  - Toxin/no toxin production, e.g., *Clostridium perfringens*
- In relation to the applied process
  - Recovery/no recovery

# Probabilistic models

## *Model structures*

Gysemans et al. (2007, IJFM) defines **four major model types**

1. Deterministic models
2. Based on the Minimum Convex Polyhedron concept
3. Logistic regression models
4. Artificial neural networks

# Probabilistic models

## *Logistic regression models*

### Ordinary logistic regression model

$$\text{logit}(p) = \left( \frac{p}{1-p} \right)$$

with p the probability of growth,  
and x & y the variables considered

$$= a_1 \cdot x + a_2 \cdot y + a_3 \cdot x^2 + a_4 \cdot y^2 + a_5 \cdot x \cdot y$$

- + Easy to fit
- + Can take many variables + interactions
- Data over-fitting is plausible

Gysemans et al. (2007, IJFM)

# Probabilistic models

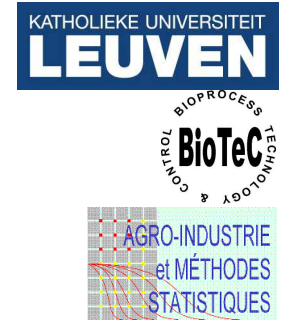
## *Overall applicability*

- Due to the mainly data-driven approach of G/NG models, the properties of the experimental data are of utmost importance, i.e., the overall validity of the model is determined by
  - The number of data/repetitions
  - The experimental region considered
  - The experimental time covered
  - The initial cell count

**=> Well-considered experimental design is required as this will define the final applicability of the probabilistic model!**

# Probabilistic models

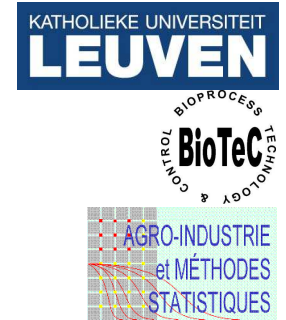
## *Design Of Experiments*



- Probabilistic models => polynomial
- Use of DOE designs for response surface models
- Polynomial (RSM) => specific DOE
  - Box-Behnken
    - Battey et al. (2002, AEM): probability of yeast spoilage of cold-filled ready-to-drink beverages

# Probabilistic models

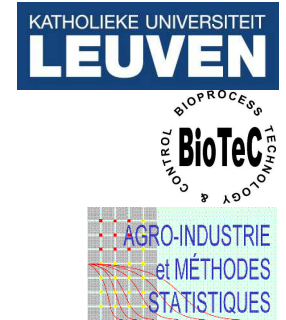
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# Probabilistic models

## *Design of Experiments*

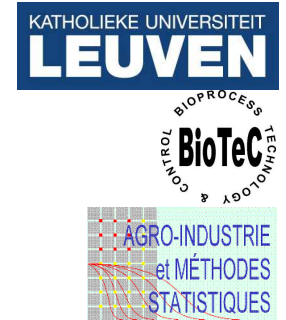


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    - Hwang (2009, FM): growth probability of *L. monocytogenes* in salmon (salt, smoke (phenol) and T)
- Almost all = full factorial design



# Probabilistic models

## *Design of Experiments*



↔ Focus is on the **event** (G/NG) boundary

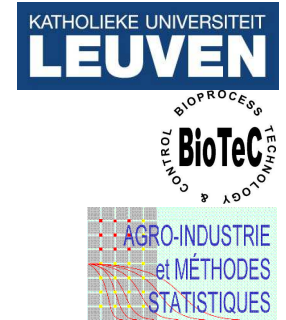
- Specific location
- Large number of samples
- Large number of replicates

→ a two-step approach

1. First approximation of the G/NG region
2. Perform large # of experiments & replicates @ G/NG

# Probabilistic models

## *Important model building aspects*



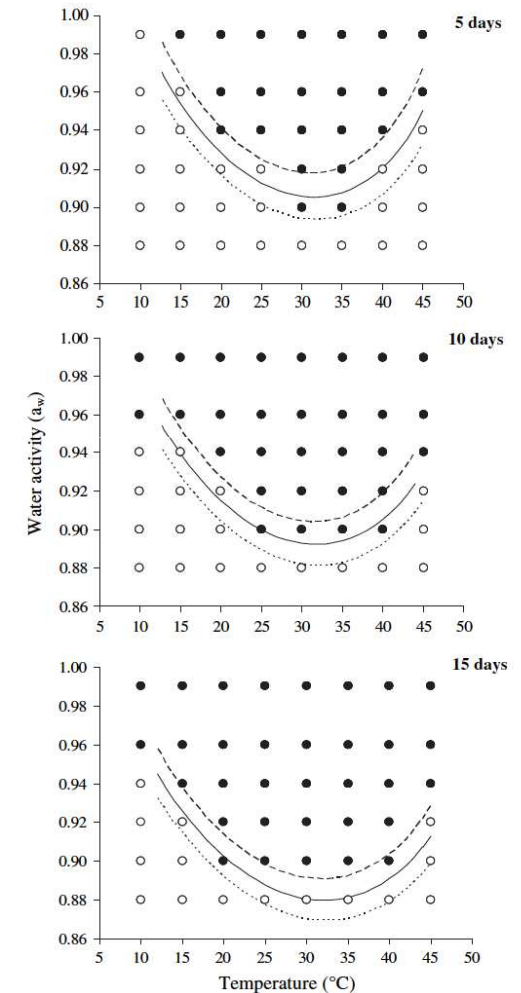
- Experimental time
- Inoculum level
- Data collection & Number of repetitions
- Model complexity: polynomial models
- Identifying the studied action: detection limit (OD)
- System characteristics: Liquid-solid

# Probabilistic models

## Experimental time

- Experimental time taken highly defines the final validity of the model
- Growth boundaries tend to shifted to harsher conditions when the time span increases

G/NG of *Byssochlamys fulva* DSM 1808 on malt extract agar at P values of 0.9 (dashed line), 0.5 (solid line), and 0.1 (dotted line). Solid symbols indicate fungal growth; open symbols indicate no growth.



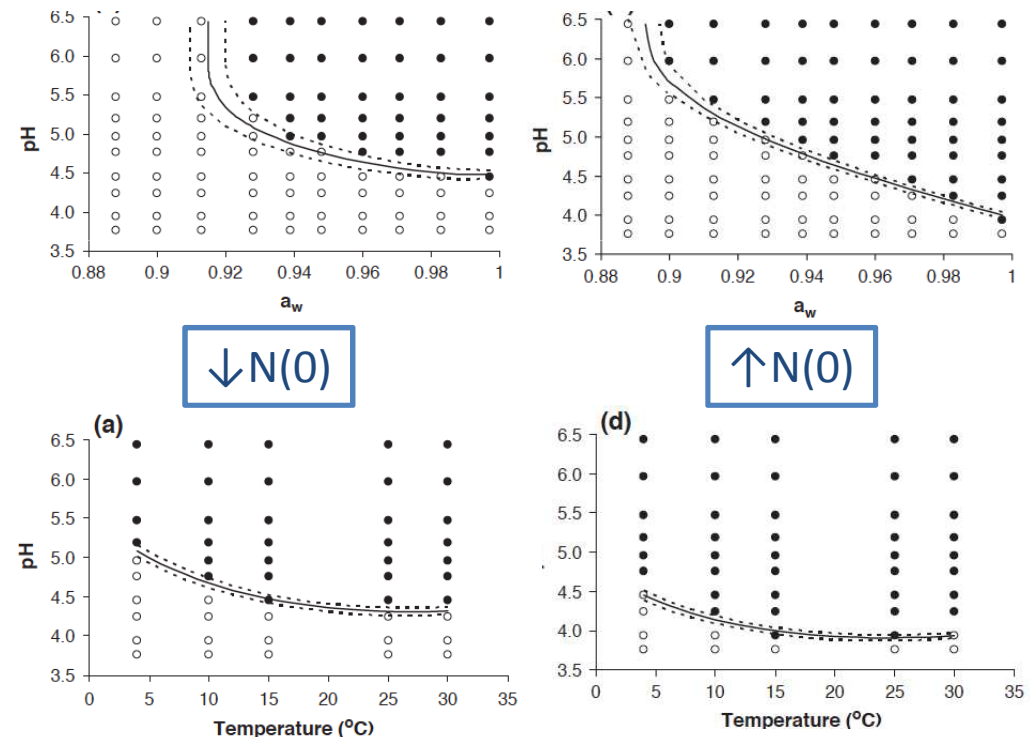
Panagou et al. (2010, IJFM)

# Probabilistic models

*Inoculum level*

**G/NG of *L. monocytogenes* => f(T, pH and  $a_w$ )**

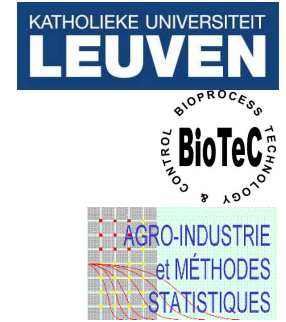
- $\neq N(0)$  => different G/NG
- $\downarrow N(0)$  => require less harsh conditions for NG
- @  $\downarrow N(0)$ : more effect of cell heterogeneity
- For pathogens:  $\downarrow N(0)$
- For spoilage:  $\uparrow N(0)$



Koutsoumanis & Sofos (2005, IJFM)

# Probabilistic models

## *Data collection & repetitions*

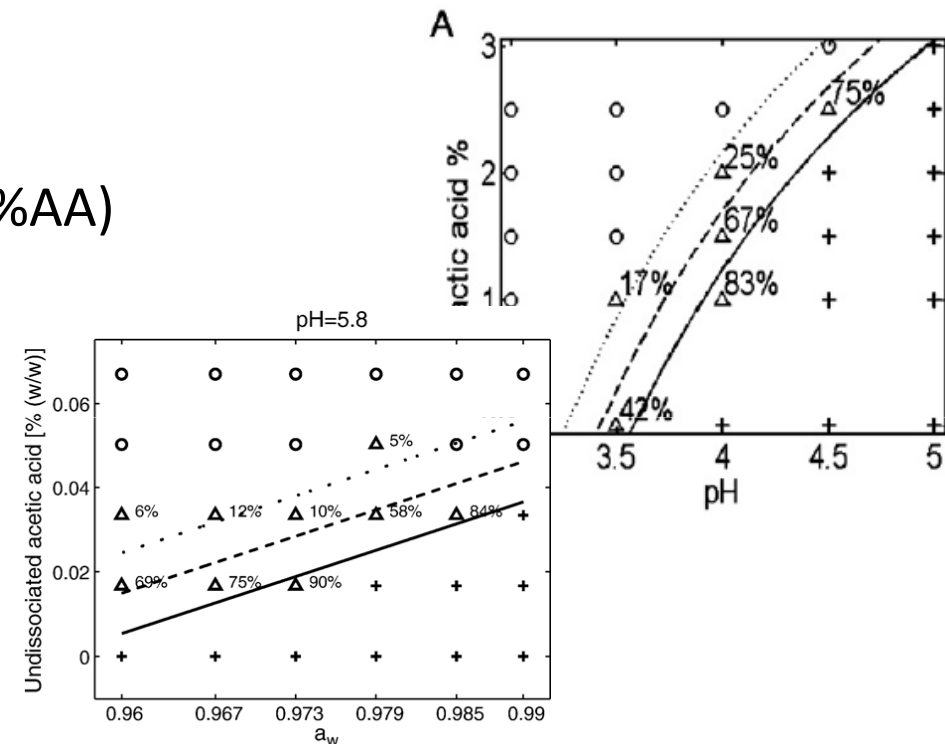


- Number of experimental data & number of repetitions highly determines the model characteristics.
- $\uparrow$  # repetitions  $\Rightarrow$  a more accurate G/NG boundary

# Probabilistic models

## *Data collection & repetitions*

- Vermeulen et al. (2009, IJFM)
  - 12 replicates => 9%
  - *Lactobacillus fructivorans* (0%AA)
- Gysemans et al. (2007, IJFM)
  - 20 replicates => 5%
  - *L. monocytogenes* (pH=5.8)



=> the experimental scheme should be a balance between

- Practical feasibility
- Required accuracy

# Probabilistic models

## *Model complexity*

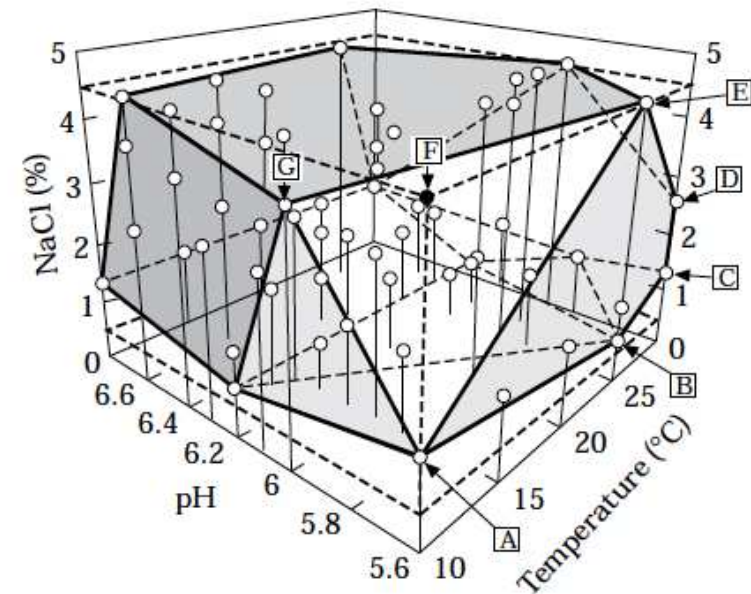
- Logistic regression models = polynomials
  - ↑# **parameters** => can fit any relation
  - Highly sensitive to parameter correlation & **over-fitting**
- **Limit the order of the polynomial**
  - Imposing constraints based on microbial knowledge (Geeraerd et al. (2004, IJFM))
  - selection of **significant model parameters**
    - Forward selection
    - Backward elimination
    - Stepwise selection

# Probabilistic models

## *Extrapolation region*

- Validity model - range of experimental data
- Straightforward for FFD
- More complex when applying another design
  - Region not easy to identify
  - Can be small
  - ER = minimum convex polyhedron

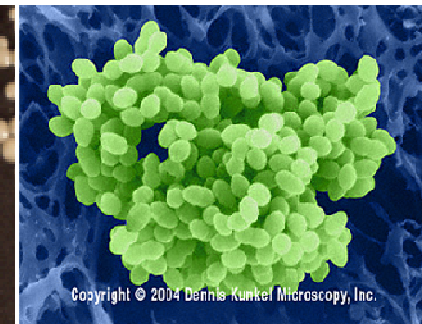
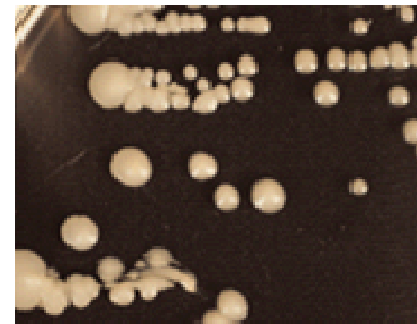
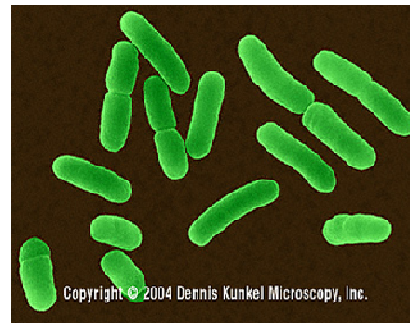
Baranyi et al. (1996, FM)





# Probabilistic models

*Food (model) system limitations*



- *planktonic* growth
- *optimal* transport:
  - nutrient → cell
  - cell → metabolites
- growth in *colonies*
- diffusion *limited* transport:
  - local nutrient depletion
  - local metabolite accumulation

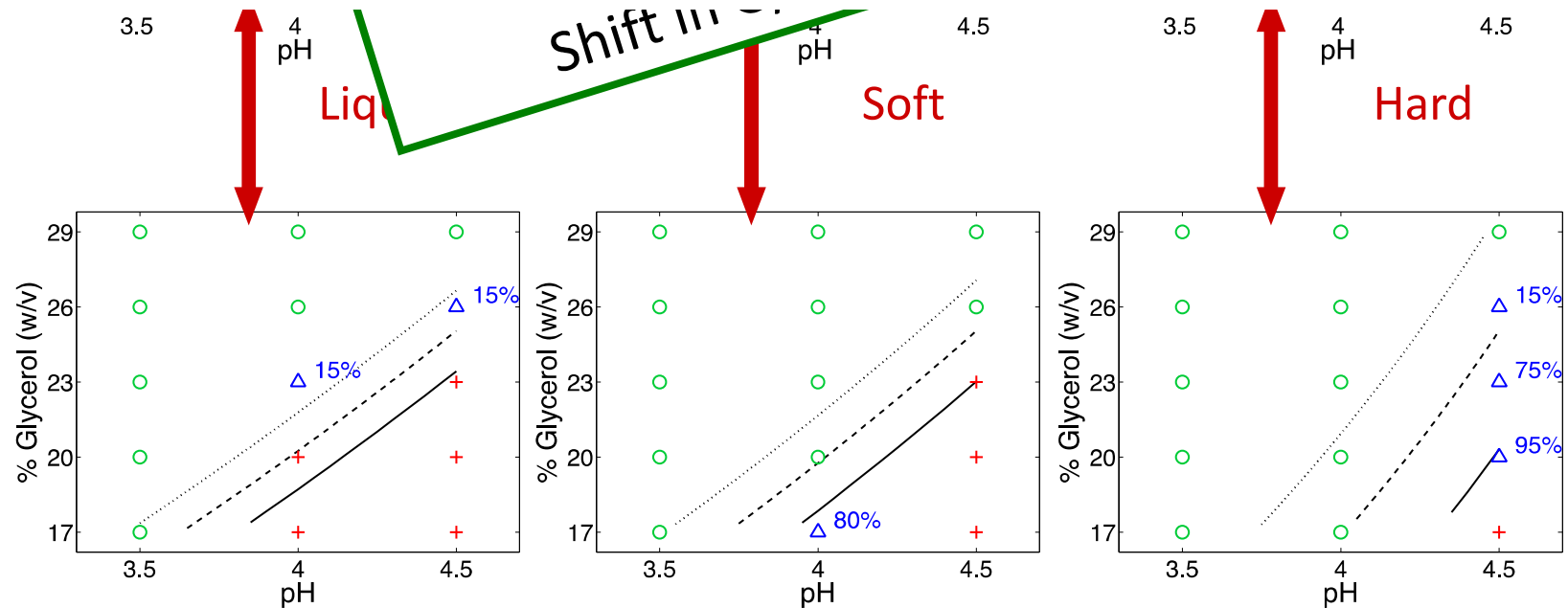
# Probabilistic models

## *Food (model) system limitations*

2,0% Acetic acid, 45 days

22°C

30°C



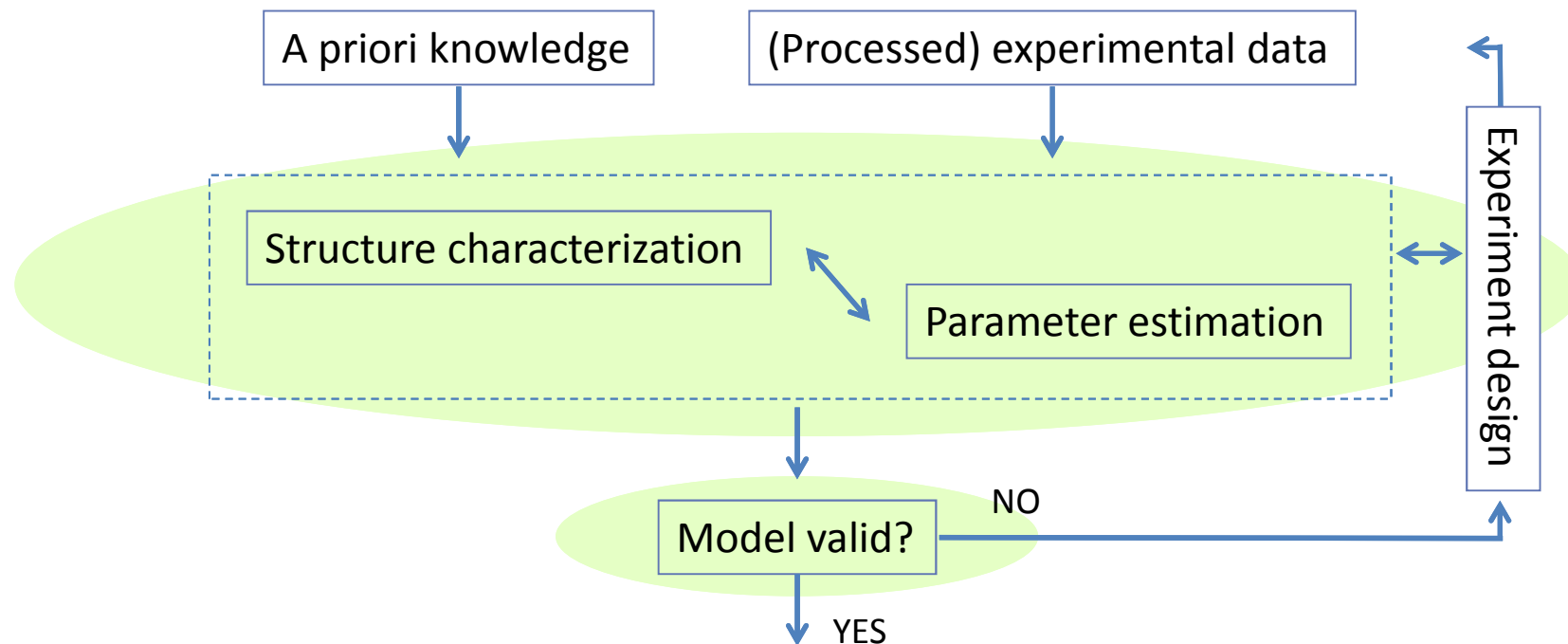
# Probabilistic models

## *Conclusions*

- PB models have a limited transferability
  - Specific strain/cocktail
  - Initial cell level => lower inoculum will require more time to reach the detection limit + different distribution of specific phenomena, e.g., the lag
  - Time span considered => longer times might finally support growth/survival/recovery/toxin production
  - Food product
- Recent publications are limited due to
  - Static character
  - High experimental load
  - Product/case specificity: liquid vs. solid character

# Conclusion

## *Importance of data collection/experimental plan*



**=> Model building is a data-driven process**

# Modeling microbial dynamics in food processes

An experiment design approach to  
predictive microbiology

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